

## Possible Existence of Alkali Metal Orthocarbonates at High Pressure

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**Abstract:** We investigate the possible existence of crystalline alkali metal orthocarbonates,  $A_4CO_4$ , where  $A = \text{Li, Na, K, Rb, and Cs}$ . We study the equilibrium between the possible modifications of the orthocarbonate  $A_4CO_4$  and the binary mixture of the possible

modifications of the alkali oxide  $A_2O$  and those of the alkali metal carbonate

$A_2CO_3$  as function of pressure. In all cases, the orthocarbonate should be stable at sufficiently high pressure ranging from 22–32 GPa ( $\text{Rb}_4\text{CO}_4$ ) to 200–220 GPa ( $\text{Cs}_4\text{CO}_4$ ).

**Keywords:** alkali metal orthocarbonates • high pressure polymorphs • structure prediction

### Introduction

Orthocarbonic acid is a tetraprotic acid and can be considered to be formed by the double hydration of carbon dioxide, which has not been observed thus far.<sup>[1]</sup> However, it has been shown computationally<sup>[2,3]</sup> that the most stable structure of  $\text{H}_4\text{CO}_4$  corresponds to a local minimum on the energy landscape with an  $S_4$  symmetry. Despite the absence of orthocarbonic acid and its salts, the orthocarbonate esters  $(\text{RO})_4\text{C}$  and  $(\text{ArO})_4\text{C}$  are well known.<sup>[1,3]</sup> The existence of these esters led to expectations that its salts, the orthocarbonates, should also be accessible.<sup>[4]</sup> Successful synthesis of the potassium, rubidium, and cesium trifluororthocarbonates  $\text{ACOF}_3$  ( $A = \text{K, Rb, Cs}$ ) by Ostwald ripening in  $\text{CH}_3\text{CN}$  applying a  $\text{COF}_2$  pressure of 3 bar<sup>[5]</sup> support our idea that alkali metal orthocarbonates should also exist. Such compounds are of interest not only because they would fill a gap in the chemical systematics, but also because of the role they might play in the mineral forming processes in the Earth's crust and mantle at high pressure and temperature conditions.

Among the elements of the second Period, nitrogen is the only one that forms an "isolated" tetrahedral tetraoxo anion, the so-called orthonitrate.<sup>[6,7]</sup> All our attempts to synthesize alkali metal orthocarbonates from the corresponding

carbonates and oxides in analogy to orthonitrates at ambient pressure have failed thus far. Nevertheless it appears to be a natural consequence of the pressure–coordination rule<sup>[8]</sup> that under high-pressure conditions The possibility exist to convert, for example, carbonate compounds into structures containing carbon in fourfold coordination by oxygen, since higher coordination usually results in smaller molar volume, which is favored at high pressure according to Le Chatelier's principle. This has led to predictions that at very high pressures the orthocarbonate  $\text{Li}_4\text{CO}_4$  with isolated  $\text{CO}_4$  units,<sup>[4]</sup> and a post-aragonite structure of  $\text{CaCO}_3$  containing chains of  $\text{CO}_4$  tetrahedra<sup>[9]</sup> might exist.

Since the synthesis route via the application of high hydrostatic pressures appears to be promising, we have started to investigate the relevant equilibria  $\text{A}_2\text{O} + \text{A}_2\text{CO}_3 \rightleftharpoons \text{A}_4\text{CO}_4$  ( $A = \text{alkali metal}$ ) as a function of pressure using computational techniques. For this it is necessary to study the part of the enthalpy surface of the  $A/C/O$  system with composition  $\text{A}_4\text{CO}_4$  at several different pressures, in order to determine as many candidates as possible for both ambient and high pressures. Of course, such an orthocarbonate would compete with high-pressure phases of the corresponding regular carbonates plus oxides which have previously been studied.<sup>[10,11]</sup>

As a consequence the orthocarbonate system poses an additional challenge because most work on structure prediction up to now has been restricted to chemical systems, where the competing phases correspond to different modifications of the same compound. However, for essentially all classes of ternary materials, an equilibrium exists between the ternary phase and the constituting binary phases, for a given overall composition. The range of (thermodynamic) stability of such a ternary phase is a function of applied tem-

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perature and pressure. For instance, for a given overall composition, at standard pressure two binary phases might be observed, while in the high-pressure regime only one ternary compound of the prescribed composition exists.

The identification of stable phases of such systems in an efficient fashion<sup>[12,13]</sup> requires the exploration of the enthalpy landscapes of all relevant binary and ternary compounds in a given chemical system, together with a computation of the (free) enthalpy of various combinations of these compounds under the condition of constant overall composition. In earlier work, several structure candidates for  $\text{Li}_4\text{CO}_4$  have been presented.<sup>[4]</sup> However, the crucial issue of the competition between the orthocarbonate and the 1:1 mixture of the alkali metal oxide  $\text{A}_2\text{O}$  and the alkali metal carbonate  $\text{A}_2\text{CO}_3$  including both phases stable at ambient pressure and those stable at high pressures was not considered. As a first step towards addressing this issue, we have computed the pressure-phase diagrams of the alkali metal carbonates  $\text{A}_2\text{CO}_3$ <sup>[10]</sup> and the alkali metal oxides  $\text{A}_2\text{O}$ <sup>[11]</sup> ( $\text{A}=\text{Li}, \text{Na}, \text{K}, \text{Rb}, \text{Cs}$ ).

In this work, we study the enthalpy landscapes of the alkali metal orthocarbonates  $\text{A}_4\text{CO}_4$ . For each of these systems, we determine the thermodynamically stable phase as a function of pressure, and compare the enthalpies of the orthocarbonates with those of the 1:1 mixture of the corresponding oxides and carbonates.

## Methods

**Modeling the landscape:** Our general approach to the determination of structure candidates has been given in detail elsewhere.<sup>[12,14]</sup> A summary of the procedure is given here: The structure candidates that should be capable of existence, at least at low temperatures, correspond to local minima of the enthalpy hypersurface ( $H = E_{\text{pot}} + pV$ ) of the chemical system under investigation. Finding these candidates requires the use of a global optimization method as well as local optimization procedures, since we permit free variation of atom positions, cell parameters, ionic charges and composition, during the global landscape exploration. Since global optimization methods, in general, involve many millions of energy evaluations for atomic configurations, one usually cannot perform the energy calculations using *ab initio* methods. Therefore, we modeled the systems as spherical ions that interact via a simple empirical two-body interaction potential,  $V_{ij}(r_{ij})$ , consisting of a Coulomb and a Lennard-Jones term that depend only on the atom–atom distance  $r_{ij}$  in order to allow fast calculations of the energy,  $E_{\text{pot}} = \sum_{i < j} V_{ij}(r_{ij})$ , of a given configuration:

$$V_{ij}(r_{ij}) = \frac{q_i q_j}{r_{ij}} \exp(-\mu r_{ij}) + \varepsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] \quad (1)$$

The parameters entering the empirical potential are the sum of the ionic radii multiplied by a scaling factor  $r_s$ ,  $\sigma_{ij} =$

$r_s(r_{\text{ion}}(i) + r_{\text{ion}}(j))$ , the parameters  $\varepsilon_{ij}$ , and the convergence parameter  $\mu$ . The ionic radii of the metal cations employed during the landscape explorations in this work were taken from Emsley:<sup>[15]</sup>  $r_{\text{ion}}(\text{Li}^+) = 0.78 \text{ \AA}$ ,  $r_{\text{ion}}(\text{Na}^+) = 0.98 \text{ \AA}$ ,  $r_{\text{ion}}(\text{K}^+) = 1.33 \text{ \AA}$ ,  $r_{\text{ion}}(\text{Rb}^+) = 1.49 \text{ \AA}$ ,  $r_{\text{ion}}(\text{Cs}^+) = 1.65 \text{ \AA}$ . Furthermore, we used  $r_s = 1.1$ ,  $\varepsilon_{ij} = 0.4$  and  $\mu = 0.1$ .

Since we are only interested in those modifications in the A/C/O system, which consist of metal cations and  $\text{CO}_4$ -complex anions, we employed fixed  $(\text{CO}_4)^{4-}$  building units during the global optimizations. The building unit was treated as rigid with fixed charge distribution for each individual optimization run, and we used two limiting charge distributions, ( $q(\text{C}) = +4$ ,  $q(\text{O}) = -2$ ) and ( $q(\text{C}) = 0$ ,  $q(\text{O}) = -1$ ), and a tetrahedral shape analogous to  $\text{SiO}_4$  units in crystalalite.

Since this structural unit has not yet been observed within an extended solid, we have previously optimized the size of the building units over a range of C–O distances, that is,  $d(\text{C–O}) = 1.37\text{--}1.57 \text{ \AA}$ , using a feedback loop between the global and local optimization stages.<sup>[4]</sup> The lower limit of  $d(\text{C–O})$  was chosen to approximate the sum of the ionic radii of  $\text{C}^{4+}$  and  $\text{O}^{2-}$ , while the upper limit was based on the repulsion between the oxygen ions analogous to the one in the  $\text{SiO}_4$  tetrahedron in crystalalite. During the global optimization stage of the feedback loop, the building unit was treated as a rigid soft body with fixed charge distribution for each individual optimization run. The adjustment of the size of the building unit occurred by alternating empirical-potential global optimizations and *ab initio* level local optimizations for the structure candidates found in the global optimization step. The final C–O distance of  $d(\text{C–O}) = 1.42 \text{ \AA}$  is in satisfactory agreement with those experimentally determined for molecules containing a  $\text{COF}_3$  unit.<sup>[5]</sup>

Since we are interested in crystalline compounds, we have introduced periodic boundary conditions and employed up to three formula units during the global optimizations. The calculations were repeated for a number of pressures starting with a pressure of one atmosphere increasing in steps by a factor of 10 up to 1 TPa, and similarly for negative pressures up to  $-100 \text{ GPa}$ . The negative pressure range is of interest for several reasons: In many cases modifications found to be deep-lying local minima at negative pressures happen to be thermodynamically preferred phases at high temperatures at standard pressure, reminiscent of Ostwald's rule.<sup>[16]</sup> Similarly, such a modification found at negative pressures can occur as a low-temperature modification at standard pressure in one of the homologue systems.<sup>[8]</sup> Finally, such modifications can occur if the synthesis takes place under effective negative pressures, for example, crystal growth within a low-density amorphous matrix.<sup>[17]</sup>

**Optimization procedures and selection of basis sets:** The global optimizations were performed by employing the stochastic simulated annealing algorithm,<sup>[18,19]</sup> with a temperature schedule  $T_n = T_0 \gamma^n$  ( $\gamma = 0.95, \dots, 0.995$ ). The moveclass consisted of atom movement and building unit rotation (about 80% of the moves), atom exchange (5%), and random variations of the cell parameters (15%), keeping

the ionic charges fixed. In order to determine which combination of basis sets is optimal for the ab initio calculations, a number of basis sets were tested for  $A_2O$ ,  $A_2CO_3$  and  $A_4CO_4$ . Some of the basis sets were all-electron basis sets<sup>[20]</sup> (AEBS),<sup>1</sup> and some were “Stuttgart/Cologne-type” pseudo-potential basis sets<sup>[21]</sup> (PPBS), in the case of Rb (ECP28MWB), and Cs (ECP46MWB). The optimal outermost shell exponents were optimized through energy minimization of the crystal energy. The final optimized basis sets can be found in references [10] and [11].

**Weighting of phase contributions and determination of transition pressures:** In addition to the optimized cell parameters, the  $E(V)$  curves found by the local optimizations in a given chemical system  $X$  ( $X = A_2O$ ,  $A_2CO_3$  or  $A_4CO_4$ ) yield the bulk modulus  $B_0$  by fitting the calculated data points to the Murnaghan equation:<sup>[22]</sup>

$$E(V) = \frac{VB_0}{B'_0} \left[ \frac{(V_0/V)B'_0}{B'_0 - 1} + 1 \right] - C \quad (2)$$

where the four fit parameters  $B_0$  and  $B'_0$  are the bulk modulus and its derivative,  $V_0$  the equilibrium volume, and  $C$  the zero of the energy scale. By calculating the enthalpies:

$$H_i = E_i(V) + pV = E_i(V) - \frac{\partial E}{\partial V} V \quad (3)$$

for the various structure candidates  $i$ , we determine the transition pressures between different modifications  $i$  and  $j$  by setting the enthalpies equal,  $H_i = H_j$ .

For a given pressure  $p$ , the minimum of the enthalpies  $H_i^X(p)$  over all modifications  $i$  found in the system  $X$  yields the enthalpy of system  $X$  as function of pressure  $H^X(p)$ . By comparing the appropriately weighted average of  $H^{A_2O}(p)$  and  $H^{A_2CO_3}(p)$  with  $H^{A_4CO_4}(p)$ ,  $H_{\text{comb}}(p) = H^{A_2O}(p) + H^{A_2CO_3}(p)$ , we can then calculate the pressure range, where the orthocarbonate is stable against disproportionation into the corresponding oxide and the carbonate.

In practice, we first compute the combined  $E(V)$  curve of the  $A_2O$ -plus- $A_2CO_3$  system,  $E_{\text{comb}}(V)$ , via an inverse Legendre transform of  $H_{\text{comb}}(p) = H^{A_2O}(p) + H^{A_2CO_3}(p)$ . Since we have generated the enthalpies  $H^{A_2O}(p)$  and  $H^{A_2CO_3}(p)$  via Equation (3), the simple geometric construction shown in Figure 1 can be employed to generate  $E_{\text{comb}}(V)$  from  $H_{\text{comb}}(p)$ . We note that  $V = V^{A_2O}(p) + V^{A_2CO_3}(p)$ , where  $V^{A_2O}(p)$  and  $V^{A_2CO_3}(p)$  are the volumes, at which the slope of  $\partial E/\partial V$  equals  $(-p)$ . The same relation must hold true for  $E_{\text{comb}}(V)$ , which implies that  $E_{\text{comb}}(V)$  is the curve given by the set of all points  $(V, E_{\text{comb}}(V))$ , where  $V = V^{A_2O}(p) + V^{A_2CO_3}(p)$ , and

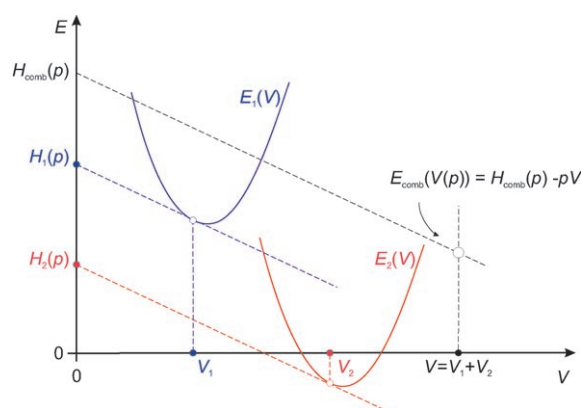


Figure 1. Construction of the point  $E_{\text{comb}}(V(p))$  of the  $E(V)$  curve representing the mixture of 1 and 2 at a given pressure  $p = -\frac{\partial E_1}{\partial V} = -\frac{\partial E_2}{\partial V} = -\frac{\partial E_{\text{comb}}}{\partial V}$  starting from the  $E(V)$  curves for the individual components and using Equation (3). The complete curve  $E_{\text{comb}}(V)$  is constructed by repeating this procedure for all pressures, and is given by the envelope of the line  $H_{\text{comb}}(p) - pV$ .

$$\begin{aligned} E_{\text{comb}}(V) &= H_{\text{comb}}(p) - pV \\ &= H^{A_2O}(p) + H^{A_2CO_3}(p) - p(V^{A_2O}(p) + V^{A_2CO_3}(p)) \\ &= E^{A_2O}(p)(V^{A_2O}(p)) + E^{A_2CO_3}(V^{A_2CO_3}(p)) \end{aligned} \quad (4)$$

Note that if we had only access to  $H_{\text{comb}}(p)$ , we would have computed  $V(p)$  via  $V = \partial H_{\text{comb}}/\partial p$ , that is:

$$E_{\text{comb}}(V) = H_{\text{comb}}(p) - p \frac{\partial H_{\text{comb}}}{\partial p} \quad (5)$$

Using  $E_{\text{comb}}(V)$  and the  $E(V)$  curves of the hypothetical modifications of  $A_4CO_4$ ,  $E_i(V)$ , we then compute the transition pressures by determining the common tangent between  $E_{\text{comb}}(V)$  and  $E_i(V)$ .

## Results

**Results of the global search:** After performing more than 2500 global optimizations with  $Z$  formula units per simulation cell ( $Z = 1, 2, 3$ ), 262 structures with space groups other than  $P1$  or  $P\bar{1}$  were observed. After elimination of duplicates, eighty seven different new structure types were found to constitute local minima on the various enthalpy landscapes. After a preliminary ranking of the structures on ab initio level, we have reduced the list of the most promising structure candidates to 52. A list of the new structure types after local optimizations employing the Hartree-Fock method is given in Tables 1–5; for DFT-B3LYP data, see Supporting Information: Tables S1.1–1.5).

The overview in Figure 2 shows that on average for each pressure, up to 45% of the optimization runs resulted in structures with space groups other than  $P1$  or  $P\bar{1}$ . The number of formula units applied in the simulation appears to have an influence on the diversity of the structure candidates, ranging from essentially 100%  $P1$  or  $P\bar{1}$  structures for

<sup>1</sup> <sup>1</sup>Li (6-1G), Na (8-511G\*), K (86-511G\*), C (6-21G\*) and O (8-411G)

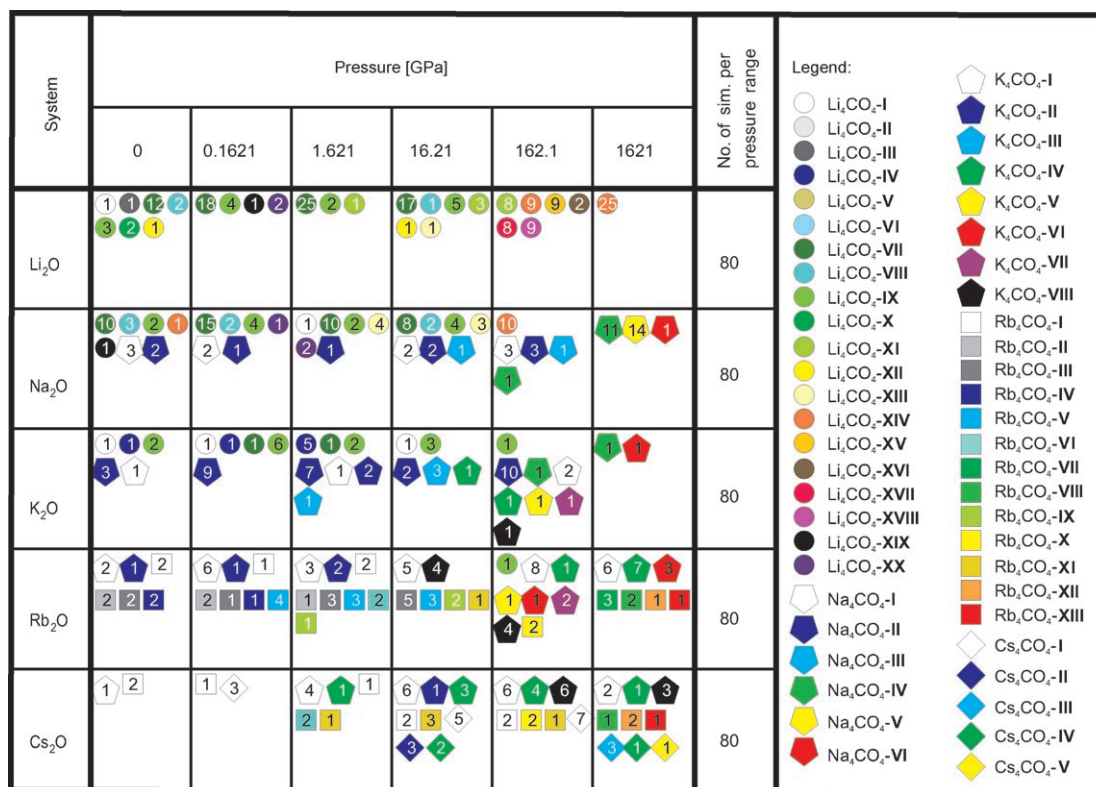


Figure 2. Distribution of the structure candidates over different pressure ranges for the  $A_4CO_4$  system ( $A = \text{Li, Na, K, Rb, and Cs}$ ). Structures with space group  $P1$  or  $P\bar{1}$  are not listed in order to avoid overloading the figure. In each entry, the different structure types are listed that were observed during the global optimization on the enthalpy landscape in the particular system at the specific pressure. Each structure type is represented by a symbol, and the number inside the symbol shows the number of times this particular local minimum had been found.

three formula units (in all systems) to about 35% for one formula unit in the case of  $\text{Li}_4\text{CO}_4$ . The number of different structure types (besides those with space group  $P1$  or  $P\bar{1}$ ) summed over all pressures for a given system ranged from 15 for  $\text{Na}_4\text{CO}_4$ , over 16 for  $\text{Rb}_4\text{CO}_4$ , 18 for  $\text{Li}_4\text{CO}_4$ , to 19 for both  $\text{K}_4\text{CO}_4$  and  $\text{Cs}_4\text{CO}_4$ . In all systems, the number of different structure candidates shows a clear peak at the high end of the intermediary pressure range, and this peak is shifted to somewhat higher pressures with increasing cation size.

Regarding the kinetic stability of these structures, we have no quantitative data, since no threshold runs<sup>[23,24]</sup> have been performed for this system. However, some of the structures were found during global optimizations over a rather wide range of pressures, indicating that they should possess a rather high degree of stability as long as the  $\text{CO}_4$  unit itself remains stable. In our earlier work,<sup>[4]</sup> we have also performed global optimizations for a wide range of pressures in the  $\text{Li}_4\text{CO}_4$  system employing carbon and oxygen atoms/ions instead of a  $\text{CO}_4$  unit together with lithium atoms/ions. These explorations have shown that for high pressures the coordination of carbon by oxygen changes from three (trigonal planar) to four (tetrahedral), suggesting that at sufficiently high pressures, the fourfold coordination will be stable.

**Results of the local optimizations:** In each system, the local refinement optimizations were performed for the most promising new candidates found during the global optimizations in the  $A_4\text{CO}_4$  system. The resulting  $E(V)$  curves, when using the HF approximation, are given in Figures 3, 5, 7, 9 and 11; the analogous curves for the DFT calculations are very similar (see Supporting Information Figures S1.1–S1.5 and Tables S1.1–S1.5). The optimized cell parameters and bulk moduli found employing the HF approximation for the selected structure candidates are given in Tables 1–5.

By comparing  $H^{A_4\text{CO}_4}(p)$  with the appropriately weighted average of  $H^{A_2\text{O}}(p)$  and  $H^{A_2\text{CO}_3}(p)$ ,  $H_{\text{comb}}(p) = H^{A_2\text{O}}(p) + H^{A_2\text{CO}_3}(p)$ , the pressure ranges where the orthocarbonate is stable against disproportionation into the corresponding oxide and the carbonate have been calculated. We find that in all systems the combined  $E(V)$  curve of the  $A_2\text{O}$ -plus- $A_2\text{CO}_3$  system at standard pressure corresponds to the thermodynamically stable structure, while at high pressures some modification of  $A_4\text{CO}_4$  should be favored. These results agree with the experimental observation that these hypothetical modifications do not appear to be thermodynamically stable at low pressures.

Unexpectedly, potassium and rubidium show relatively low transition pressures from  $A_2\text{O}$ -plus- $A_2\text{CO}_3$  to the hypothetical modifications of the  $A_4\text{CO}_4$  system. This contradicts



the usual “chemical intuition”, since if one considers the cation size to be the crucial quantity, one would expect  $\text{Li}_4\text{CO}_4$  to have the lowest transition pressure. On the other hand, the cesium cation’s basicity tends to favor a more localized type of bond, leading to the alternative expectation that  $\text{Cs}_4\text{CO}_4$  should be the first orthocarbonate to be found with increasing pressure.

One should note that several interesting hypothetical high-pressure modifications fit into a scheme suggested by Nuss<sup>[25]</sup> in the system  $\text{A}_4\text{TiX}_4$ , where he treats the  $\text{A}_4\text{TiX}_4$  unit as a neutral heterocubane. The heterocubane is the tetrahedral structural derivative of the simple cube, and even rock salt can be described as a simple cubic packing of “ $\text{Na}_4\text{Cl}_4$  heterocubanes”.<sup>[26]</sup> Since the orthocarbonates are rather complicated structures to plot and interpret from a chemical point of view we have attempted to describe our structures as 3D arrangements of heterocubanes when appropriate. The structures are shown below (see Figure 14–20).

**Results restricted to  $\text{Li}_4\text{CO}_4$ :** The mixture of  $\text{Li}_2\text{O}$  and  $\text{Li}_2\text{CO}_3$  is stable over a wide range of pressure up to about 80–110 GPa. A mixture between the  $\text{CaCl}_2$ -type ( $\text{Li}_2\text{O}$  system) and  $\gamma$ - $\text{Cs}_2\text{CO}_3$  ( $\text{Li}_2\text{CO}_3$  system) exists in the range of high effective negative pressures. Then we observe a collapse of volume due to a transition of the carbonate from the  $\gamma$ - $\text{Cs}_2\text{CO}_3$  to the  $\text{Li}_2\text{CO}_3$ -type-19 modification at moderate negative pressures. One should note that those pressures have only a meaning from a calculation point of view, since even when growing a crystalline phase inside a low-density amorphous matrix<sup>[17]</sup> experimentally only effective negative pressures of at most a few GPa can be reached. At about –10 GPa, a transition for the oxide takes place: the  $\text{CaCl}_2$  structure type undergoes a phase transition to the fluorite structure type ( $\text{CaF}_2$ -type). From approximately –5 GPa up to 10 GPa there exists a mixture of the  $\text{CaF}_2$ -type, for the oxide and the Zabujelite structure type for the carbonate. This is followed by a phase transition to the HP- $\text{Li}_2\text{CO}_3$ -type structure in the carbonate. Finally, the  $\text{CaF}_2$ -type should undergo a pressure induced phase transition to the  $\gamma$ - $\text{US}_2$  structure (for more details see refs. [10, 11]).

From Figures 3 and 4 and Table 1 (for DFT-B3LYP data see Supporting Information Figure S1.1 and Table S1.1), we see that in the  $\text{Li}_4\text{CO}_4$  system it should be possible to synthesize

orthocarbonates for pressures between 80–110 GPa. According to our calculations a phase transition should occur from a mixture of the  $\gamma$ - $\text{US}_2$ -type modification of  $\text{Li}_2\text{O}$  and the HP- $\text{Li}_2\text{CO}_3$  phase for  $\text{Li}_2\text{CO}_3$  to the  $\text{Li}_4\text{CO}_4$ -X in the  $\text{Li}_4\text{CO}_4$  system. As we discussed in earlier work,<sup>[27]</sup> one would expect from general considerations, that the Hartree–Fock calculations produce larger equilibrium volumes and higher transition pressures than the DFT ones, with the experimental values lying somewhere in-between. The predicted transition pressure is rather high and is most likely the reason why all attempts to synthesize  $\text{Li}_4\text{CO}_4$  in the range of pressures up to 50 GPa<sup>[28]</sup> have failed thus far. The possible high-pressure structures in the  $\text{Li}_4\text{CO}_4$  system are shown below (see Figure 14). According to nomenclature introduced in references [25] and [26], the structure  $\text{Li}_4\text{CO}_4$ -X belongs to the  $I2(I)$  arrangement of heterocubanes. Table 1 and Table S1.1 in the Supporting Information show structural data, minimum volumes, bulk moduli and energies of selected structure candidates for the  $\text{Li}_4\text{CO}_4$  system after local optimizations on Hartree–Fock and DFT-B3LYP basis, respectively.

**Results restricted to  $\text{Na}_4\text{CO}_4$ :** Similar to the  $\text{Li}_4\text{CO}_4$  system, the most promising structure candidates found for  $\text{Na}_4\text{CO}_4$  were chosen for refinement optimizations. The  $E(V)$  curves were computed and are shown in Figure 5 and Table 2 (for DFT-B3LYP data see Supporting Information Figure S1.3 and Table S1.2). The transition to the orthocarbonates should occur at 37–60 GPa (cf. Figure 6). In the case of the  $\text{Na}_4\text{CO}_4$  system we have observed a number of phase transitions. As we can see in Figure 5, in the range of very high

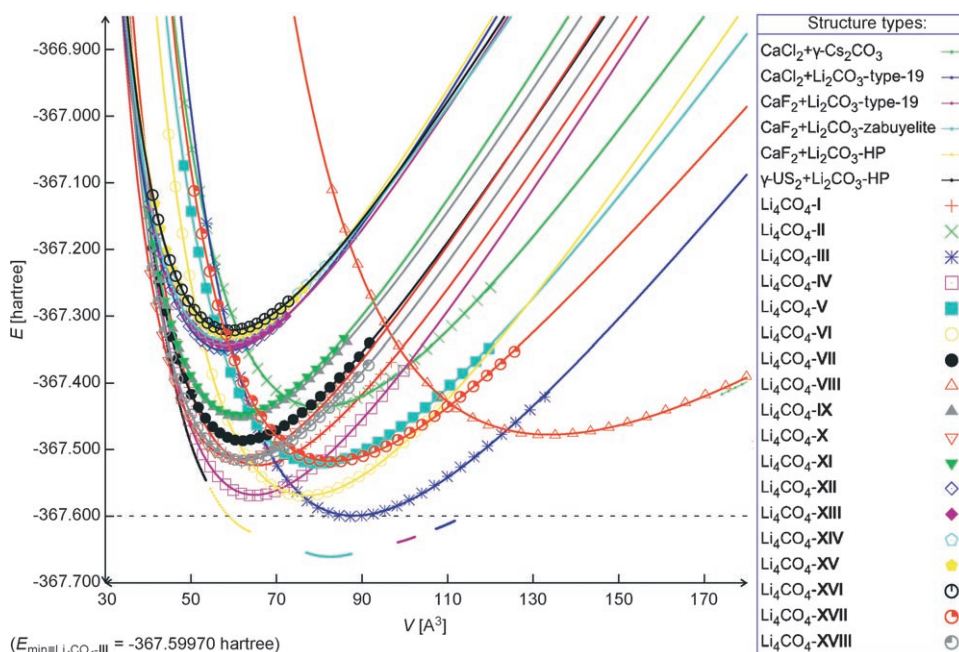


Figure 3.  $E(V)$  curves for selected structure candidates calculated on ab initio level (HF) in the  $\text{Li}_4\text{CO}_4$  system together with the combined curve for  $\text{Li}_2\text{O} + \text{Li}_2\text{CO}_3$ . The dashed horizontal line refers to the energy minimum of the  $\text{Li}_4\text{CO}_4$  system ( $E_{\min}$ ).

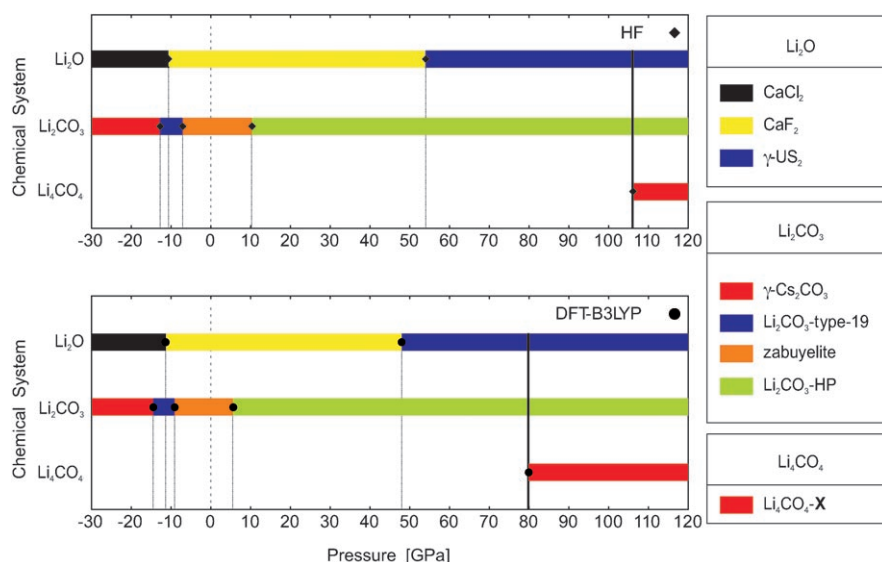


Figure 4. Low-temperature modifications of  $\text{Li}_4\text{CO}_4$  as function of pressure in equilibrium with the solid state reaction  $\text{Li}_2\text{O} + \text{Li}_2\text{CO}_3$ . Only the modifications with the lowest enthalpy are depicted. Upper box: HF. Lower box: DFT-B3LYP.

negative pressures a  $\text{CaCl}_2$  oxide modification exists together with  $\gamma\text{-Cs}_2\text{CO}_3$  (green line), and then a  $\beta\text{-Rb}_2\text{CO}_3$  (blue line) and  $\alpha\text{-Na}_2\text{CO}_3$  (magenta line) carbonate modification. The next phase transition for the oxide is from the  $\text{CaCl}_2$ - to the  $\text{CaF}_2$ -structure type. Short cyan and yellow lines show the transition between the  $\alpha\text{-Na}_2\text{CO}_3$ - and the  $\beta\text{-Na}_2\text{CO}_3$ -carbonate modification with the oxide in the  $\text{CaF}_2$ -structure type. In the range of pressures between  $-5$  GPa to  $5$  GPa (about  $10$  GPa according to HF calculations) we find the oxide  $\text{CaF}_2$ - and the carbonate  $\gamma\text{-Na}_2\text{CO}_3$  modification. Upon increasing pressure, several phase

Table 1. Data for structure candidates for  $\text{Li}_4\text{CO}_4$  after local optimizations on ab initio level (HF).

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	x	y	z		
$P\bar{4}3m$ (215) cubic	$a = 4.03079$	C1(1b)	0.5	0.5	0.5	65.489	-367.5238
	$\alpha = \beta = \gamma = 90$	O1(4e)	0.29764	0.29764	0.29764	164.017	
$\text{Li}_4\text{CO}_4\text{-I}$ $R\bar{3}m$ (160) trigonal	$a = 4.32623$	C1(1a)	0.99961	0.99961	0.99961	80.020	-367.4370
	$\alpha = \beta = \gamma = 84.77741$	O1(3b)	0.81909	0.19316	0.81909	142.917	
$\text{Li}_4\text{CO}_4\text{-II}$		O2(1a)	0.16322	0.16322	0.16322		
		Li1(1a)	0.71409	0.71409	0.71409		
$\bar{I}\bar{4}2m$ (121) tetragonal	$a = 6.39767$	Li2(3b)	0.49861	0.10286	0.49861	175.659	-367.5997
	$c = 4.29166$	C1(2b)	0	0	0.5	126.680	
$\text{Li}_4\text{CO}_4\text{-III}$ $\bar{I}\bar{4}2m$ (121) tetragonal	$\alpha = \beta = \gamma = 90$	O1(8i)	0.12253	0.12253	0.30592		
	$a = 4.04978$	Li1(8i)	0.82438	0.82438	0.85875		
$\text{Li}_4\text{CO}_4\text{-IV}$ $Cm$ (8) monoclinic	$a = 6.55195$	C1(2a)	0	0	0	129.690	-367.5686
	$b = 6.33513$	O1(8i)	0.79583	0.79583	0.90050	167.560	
$\text{Li}_4\text{CO}_4\text{-V}$ monoclinic	$a = 6.55195$	Li1(8i)	0.69676	0.69676	0.14250		-367.5201
	$b = 6.33513$	C1(2a)	0.00348	0	0.49870	159.491	
$\text{Li}_4\text{CO}_4\text{-VI}$ monoclinic	$c = 3.85795$	O1(4b)	0.00048	0.81681	0.69332	137.759	
	$\alpha = \gamma = 90$	O2(2a)	0.81207	0	0.24347		
$\text{Li}_4\text{CO}_4\text{-VII}$ monoclinic	$\beta = 95.13547$	O3(2a)	0.18915	0	0.35486		
		Li1(4b)	0.31427	0.21696	0.00993		
$C2$ (5) monoclinic	$a = 8.09241$	Li2(4b)	0.20302	0.70794	0.47902		-367.5692
	$b = 4.46021$	C1(2a)	0	0.22106	0	153.522	
$\text{Li}_4\text{CO}_4\text{-VIII}$ monoclinic	$c = 4.39575$	O1(4c)	0.87897	0.04668	0.08557	148.057	
	$\alpha = \gamma = 90$	O2(4c)	0.08652	0.41015	0.25390		
$\text{Li}_4\text{CO}_4\text{-IX}$ monoclinic	$\beta = 104.62042$	Li1(4c)	0.31673	0.60461	0.44660		-367.4861
	$a = 5.30896$	Li2(4c)	0.13494	0.63680	0.90308		
$\text{Li}_4\text{CO}_4\text{-X}$ monoclinic	$a = 5.30896$	C1(2a)	0.47214	0	0.55192	124.980	-367.4861
	$b = 5.98005$	O1(2a)	0.30191	0	0.73538	166.404	
$\text{Li}_4\text{CO}_4\text{-XI}$ monoclinic	$c = 4.43162$	O2(4b)	0.40212	0.19977	0.33911		
	$\alpha = \gamma = 90$	O3(2a)	0.77490	0	0.79577		
$\text{Li}_4\text{CO}_4\text{-XII}$ monoclinic	$\beta = 117.33880$	Li1(2a)	0.67213	0	0.28867		
		Li2(2a)	0.07626	0	0.25643		
$C2$ (5) monoclinic	$a = 9.11258$	Li3(4b)	0.56275	0.72981	0.81968	267.186	-367.4780
	$b = 3.91271$	C1(2b)	0	0.60555	0.5	73.878	
$\text{Li}_4\text{CO}_4\text{-XIII}$ monoclinic	$c = 7.50333$	O1(4c)	0.48856	0.31775	0.65616		
	$\alpha = \gamma = 90$	O2(4c)	0.37139	0.89447	0.47686		
$\text{Li}_4\text{CO}_4\text{-XIV}$ monoclinic	$\beta = 92.90730$	Li1(4c)	0.48814	0.82740	0.69961		
		Li2(4c)	0.33740	0.38760	0.47157		

Table 1. (Continued)

Space group (no.) crystal system, type	Lattice constants ( <i>a, b, c</i> [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	<i>x</i>	<i>y</i>	<i>z</i>		
<i>R3m</i> (160) trigonal <b>Li<sub>4</sub>CO<sub>4</sub>-IX</b>	<i>a</i> = 3.99573 <i>a</i> = <i>β</i> = <i>γ</i> = 98.17150	C1(1a)	0.51019	0.51019	0.51019	61.642 166.885	−367.4516
		O1(3b)	0.29134	0.29134	0.68906		
		O2(1a)	0.76449	0.76449	0.76449		
		Li1(3b)	0.78601	0.78601	0.27705		
		Li2(1a)	0.18787	0.18787	0.18787		
<i>C2</i> (5) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-X</b>	<i>a</i> = 8.42360 <i>b</i> = 3.90118 <i>c</i> = 4.06293 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 114.02130	C1(2a)	0	0.81063	0	121.953 170.893	−367.5144
		O1(4c)	0.39064	0.09003	0.69800		
		O2(4c)	0.61150	0.52998	0.88541		
		Li1(4c)	0.63308	0.58821	0.41584		
		Li2(4c)	0.63721	0.03126	0.83017		
<i>Cm</i> (8) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XI</b>	<i>a</i> = 5.23401 <i>b</i> = 5.97460 <i>c</i> = 3.95016 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 96.94540	C1(2a)	0.99962	0	0.60672	122.619 170.300	−367.4469
		O1(4b)	0.51033	0.29793	0.38925		
		O2(2a)	0.75346	0	0.75886		
		O3(2a)	0.21916	0	0.88522		
		Li1(2a)	0.31680	0	0.40552		
<i>Cm</i> (8) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XII</b>	<i>a</i> = 5.06964 <i>b</i> = 6.10094 <i>c</i> = 3.95496 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 107.98160	Li2(4b)	0.43371	0.24098	0.87994	116.350 179.714	−367.3515
		Li3(2a)	0.72041	0	0.26351		
		C1(2a)	0.91363	0	0.48026		
		O1(4b)	0.46599	0.70937	0.71905		
		O2(2a)	0.11847	0	0.25718		
<i>Cm</i> (8) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XIII</b>	<i>a</i> = 5.54844 <i>b</i> = 5.67002 <i>c</i> = 4.04379 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 112.38560	O3(2a)	0.61036	0	0.22877	117.630 173.609	−367.3442
		Li1(2a)	0.28361	0	0.79255		
		Li2(4b)	0.33729	0.25108	0.69167		
		Li3(2a)	0.66545	0	0.74117		
		C1(2a)	0.68497	0	0.41084		
<i>Pmn</i> <sub>2</sub> (31) orthorhombic <b>Li<sub>4</sub>CO<sub>4</sub>-XIV</b>	<i>a</i> = 5.99085 <i>b</i> = 4.01834 <i>c</i> = 4.81059 <i>α</i> = <i>β</i> = <i>γ</i> = 90	O1(4b)	0.23723	0.27556	0.64950	115.807 176.800	−367.3365
		O2(2a)	0.39552	0	0.14848		
		O3(2a)	0.86510	0	0.19789		
		Li1(4b)	0.10967	0.76843	0.10759		
		Li2(2a)	0.47684	0	0.69234		
<i>Pc</i> (7) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XV</b>	<i>a</i> = 4.24568 <i>b</i> = 5.68262 <i>c</i> = 5.76918 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 121.52540	Li3(2a)	0.03061	0	0.72036	118.647 181.629	−367.3289
		C1(2a)	0	0.31488	0.33828		
		O1(2a)	0	0.62994	0.15139		
		O2(4b)	0.78894	0.10490	0.27753		
		O3(2a)	0	0.42196	0.64743		
<i>Pc</i> (7) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XV</b>	<i>a</i> = 4.24568 <i>b</i> = 5.68262 <i>c</i> = 5.76918 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 121.52540	Li1(2a)	0	0.07319	0.95632	118.647 181.629	−367.3289
		Li2(4b)	0.74533	0.59738	0.42713		
		Li3(2a)	0	0.91688	0.55454		
		C1(2a)	0.15995	0.22280	0.28843		
		O1(2a)	0.20064	0.95623	0.33259		
<i>Cmc</i> <sub>2</sub> (36) orthorhombic <b>Li<sub>4</sub>CO<sub>4</sub>-XVI</b>	<i>a</i> = 5.83423 <i>b</i> = 7.83887 <i>c</i> = 5.18436 <i>α</i> = <i>β</i> = <i>γ</i> = 90	O2(2a)	0.49622	0.31868	0.28930	237.101 170.137	−367.3216
		O3(2a)	0.12975	0.33589	0.51644		
		O4(2a)	0.81216	0.27487	0.01175		
		Li1(2a)	0.79382	0.55401	0.195280		
		Li2(2a)	0.58377	0.13209	0.63821		
<i>C2</i> (5) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XVII</b>	<i>a</i> = 9.18281 <i>b</i> = 3.88289 <i>c</i> = 6.23464 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 131.81910	Li3(2a)	0.83940	0.05177	0.43795	165.671 123.088	−367.5180
		Li4(2a)	0.30856	0.60528	0.39874		
		C1(4a)	0	0.34269	0.35112		
		O1(8b)	0.71592	0.95173	0.29390		
		O2(4a)	0	0.18282	0.17372		
<i>C2</i> (5) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XVIII</b>	<i>a</i> = 8.51852 <i>b</i> = 3.99771 <i>c</i> = 7.84632 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 152.15270	O3(4a)	0	0.28758	0.63842	124.815 165.873	−367.5164
		Li1(8b)	0.73916	0.20876	0.42484		
		Li2(4a)	0	0.43034	0.01613		
		Li3(4a)	0	0.96461	0.99771		
		C1(2b)	0	0.04704	0.5		
<i>C2</i> (5) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XVIII</b>	<i>a</i> = 9.18281 <i>b</i> = 3.88289 <i>c</i> = 6.23464 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 131.81910	O1(4c)	0.86458	0.83189	0.24796	124.815 165.873	−367.5164
		O2(4c)	0.89321	0.26074	0.54414		
		Li1(4c)	0.17670	0.33424	0.82336		
		Li2(4c)	0.13616	0.76511	0.44416		
		C1(2b)	0	0.82512	0.5		
<i>C2</i> (5) monoclinic <b>Li<sub>4</sub>CO<sub>4</sub>-XVIII</b>	<i>a</i> = 8.51852 <i>b</i> = 3.99771 <i>c</i> = 7.84632 <i>α</i> = <i>γ</i> = 90 <i>β</i> = 152.15270	O1(4c)	0.76663	0.03642	0.37302	124.815 165.873	−367.5164
		O2(4c)	0.81161	0.61511	0.20056		
		Li1(4c)	0.68802	0.55369	0.32375		
		Li2(4c)	0.74735	0.10620	0.11248		
		C1(2b)	0	0.82512	0.5		

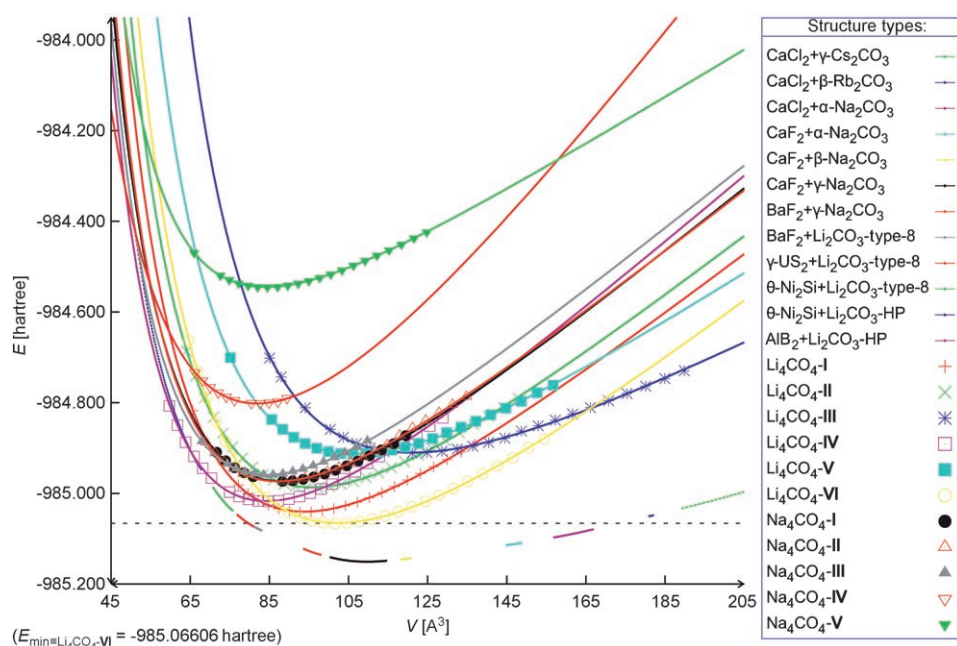


Figure 5.  $E(V)$  curves for selected structure candidates calculated on ab initio level (HF) in the  $\text{Na}_4\text{CO}_4$  system together with the combined curve for  $\text{Na}_2\text{O}+\text{Na}_2\text{CO}_3$ . The dashed horizontal line refers to the energy minimum of the  $\text{Na}_4\text{CO}_4$  system ( $E_{\min}$ ).

transitions occur in the oxide-carbonate mixture (see Figures 5 and 6), until finally between 37 GPa (DFT-B3LYP) and 60 GPa (HF) a transition to the orthocarbonate phase  $\text{Li}_4\text{CO}_4\text{-IV}$  take place. As in the case of the  $\text{Li}_4\text{CO}_4$  system, the DFT-B3LYP calculations show a lower value of the transition pressure than the Hartree-Fock ones. The possible high-pressure structure in the  $\text{Na}_4\text{CO}_4$  system is shown below (see Figure 15). It appears to belong to the  $cP1$  arrangement of heterocubanes (see refs. [25] and [25]). Table 2 and Table S1.2 (Supporting Information) show structural data, minimum volumes, bulk moduli and energies of the selected structure candidates for the  $\text{Na}_4\text{CO}_4$  system after local optimizations on Hartree-Fock and DFT-B3LYP level.

Table 2. Data for structure candidates for  $\text{Na}_4\text{CO}_4$  after local optimizations on ab initio level (HF).

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	$x$	$y$	$z$		
$P\bar{4}3m$ (215) cubic	$a = 4.54337$ $\alpha = \beta = \gamma = 90$	C1(1b)	0.5	0.5	0.5	93.785	-985.0409
$\text{Li}_4\text{CO}_4\text{-I}$		O1(4e)	0.31764	0.31764	0.31764	121.319	
$R\bar{3}m$ (160) trigonal	$a = 4.59298$ $\alpha = \beta = \gamma = 84.77761$	Na1(4e)	0.78955	0.78955	0.78955		
$\text{Li}_4\text{CO}_4\text{-II}$		C1(1a)	0.99961	0.99961	0.99961	95.754	-984.9874
		O1(3b)	0.81909	0.81909	0.19316	120.993	
		O2(1a)	0.16322	0.16322	0.16322		
		Na1(1a)	0.71409	0.71409	0.71409		
		Na2(3b)	0.49861	0.49861	0.10286		
$I\bar{4}2m$ (121) tetragonal	$a = 7.74088$ $c = 4.03695$	C1(2b)	0	0	0.5	241.899	-984.9108
$\text{Li}_4\text{CO}_4\text{-III}$	$\alpha = \beta = \gamma = 90$	O1(8i)	0.62481	0.62481	0.79119	86.664	
$I\bar{4}2m$ (121) tetragonal	$a = 4.37208$ $c = 8.81221$	Na1(8i)	0.33614	0.33614	0.28782		
$\text{Li}_4\text{CO}_4\text{-IV}$	$\alpha = \beta = \gamma = 90$	C1(2a)	0	0	0	168.446	-985.0176
$Cm$ (8) monoclinic	$a = 7.21635$ $b = 7.08114$ $c = 4.18698$ $\alpha = \gamma = 90$ $\beta = 95.13547$	O1(8i)	0.79583	0.79583	0.90050	137.398	
$\text{Li}_4\text{CO}_4\text{-V}$		Na1(8i)	0.69676	0.69676	0.14250		
		C1(2a)	0.00348	0	0.49870	213.095	-984.9128
		O1(4b)	0.00048	0.81681	0.69332	105.035	
		O2(2a)	0.81207	0	0.24347		
		O3(2a)	0.18915	0	0.35486		
		Na1(4b)	0.31427	0.21696	0.00993		
		Na2(4b)	0.20302	0.70794	0.47902		
$C2$ (5) monoclinic	$a = 8.96311$ $b = 4.97964$ $c = 4.87118$ $\alpha = \gamma = 90$ $\beta = 110.12676$	C1(2a)	0	0.19884	0	204.139	-985.0661
$\text{Li}_4\text{CO}_4\text{-VI}$		O1(4c)	0.88594	0.03452	0.03816	114.722	
		O2(4c)	0.08178	0.37127	0.25455		
		Na1(4c)	0.26804	0.67518	0.32553		
		Na2(4c)	0.11886	0.62838	0.77025		
$R\bar{3}$ (146) trigonal	$a = 4.45335$ $\alpha = \beta = \gamma = 88.09780$	C1(1a)	0.12305	0.12305	0.12305	88.178	-984.9734
$\text{Na}_4\text{CO}_4\text{-I}$		O1(3b)	0.98591	0.31795	0.87406	126.426	
		O2(1a)	0.31070	0.31070	0.31070		
		Na1(1a)	0.84400	0.84400	0.84400		
		Na2(3b)	0.33876	0.83598	0.47403		



Table 2. (Continued)

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	$x$	$y$	$z$		
<i>Cm</i> (8) monoclinic $\text{Na}_4\text{CO}_4$ -II	$a = 5.89419$ $b = 6.62708$ $c = 4.47056$ $\alpha = \gamma = 90$ $\beta = 91.86530$	C1(2a)	0.99963	0	0.43508	174.533	-984.9739
		O1(2a)	0.16335	0	0.18105		
		O2(2a)	0.76084	0	0.30381	129.972	
		O3(4b)	0.03738	0.18733	0.62191		
		Na1(4b)	0.95459	0.72226	0.14556		
		Na2(2a)	0.74955	0	0.79700		
Na3(2a)	0.34410	0	0.61765	168.898	-984.9592		
C1(2a)	0.89377	0	0.56075				
O1(4b)	0.95928	0.19190	0.76476				
O2(2a)	0.02309	0	0.31257				
O3(2a)	0.63709	0	0.41246				
Na1(2a)	0.27477	0	0.77034				
Na2(2a)	0.69896	0	0.92846	81.849	-984.8018		
Na3(4b)	0.80296	0.71462	0.26562				
C1(1a)	0.62687	0.62687	0.62687				
O1(3b)	0.32467	0.52206	0.80594				
O2(1a)	0.85054	0.85054	0.85054				
Na1(3b)	0.02588	0.79582	0.36314				
Na2(1a)	0.29818	0.29818	0.29818	150.314			
C1(1a)	0.81708	0.81708	0.81708				
O1(3b)	0.92787	0.16364	0.63511				
O2(1a)	0.54686	0.54686	0.54686				
Na1(3b)	0.66881	0.41534	0.03897				
Na2(1a)	0.16853	0.16853	0.16853				

Results restricted to  $\text{K}_4\text{CO}_4$ : Following the same approach as in the cases of  $\text{Li}_4\text{CO}_4$  and  $\text{Na}_4\text{CO}_4$  we performed ab initio local optimizations of the  $\text{K}_4\text{CO}_4$  system. The  $E(V)$  curves and structural data are shown in the Figure 7 and Table 3

(for DFT-B3LYP data see Supporting Information, Figure S1.5 and Table S1.3). Again, we found the same general trends with respect to the relation between transition pressure and choice of ab initio method as in the  $\text{Li}_4\text{CO}_4$  and

$\text{Na}_4\text{CO}_4$  systems. As we have observed in other systematic exploration of the alkali metal systems (see refs. [10], [11], [27] and [29]), potassium-based compounds exhibit many phase transitions over a comparatively small range of pressures (see e.g. ref. [27]). In these cases, the influence of temperature can affect our ability to predict exactly the sequence of phase transitions. But in the case of the orthocarbonate, the transition pressures are relatively high and the number of competing phases of the oxides and carbonates decreases. According to our calculations, a direct transition from the  $\theta$ - $\text{Ni}_2\text{Si}$  modification in the  $\text{K}_2\text{O}$  system plus the  $\gamma$ - $\text{Na}_2\text{CO}_3$  modification in the  $\text{K}_2\text{CO}_3$  system to the  $\text{K}_4\text{CO}_4$ -III structure should occur in the range of pressures

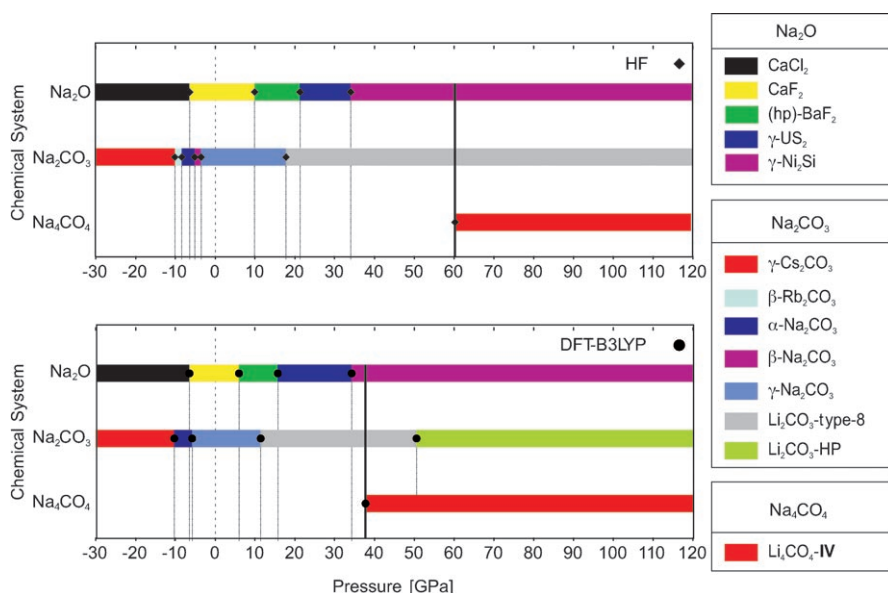


Figure 6. Low-temperature modifications of  $\text{Na}_4\text{CO}_4$  as function of pressure in equilibrium with the solid state reaction  $\text{Na}_2\text{O} + \text{Na}_2\text{CO}_3$ . Only the modifications with the lowest enthalpy are depicted. Upper box: HF. Lower box: DFT-B3LYP.

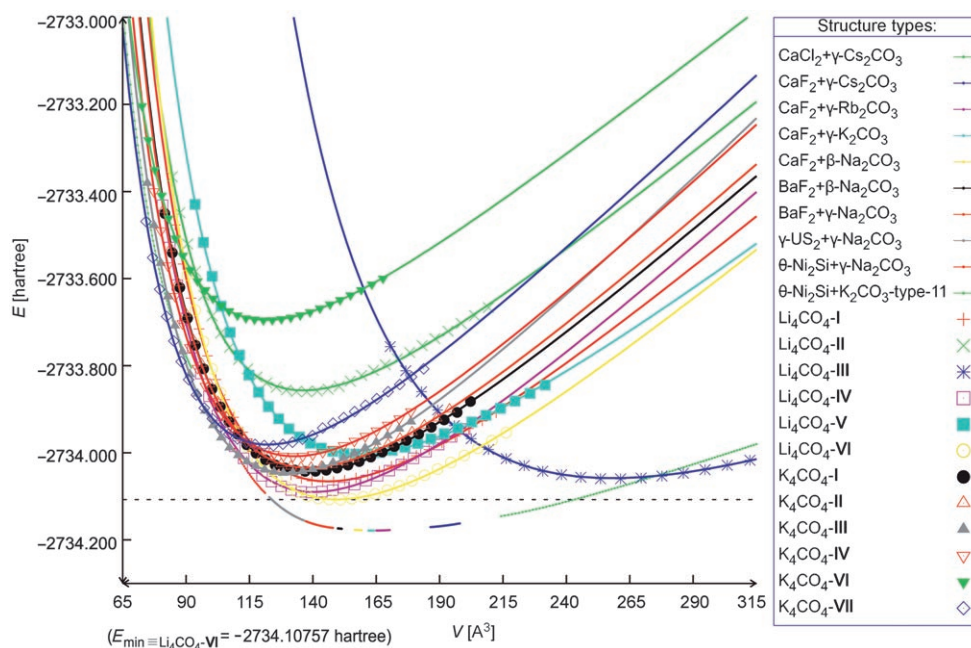


Figure 7.  $E(V)$  curves for selected structure candidates calculated on ab initio level (HF) in the  $K_4CO_4$  system together with the combined curve for  $K_2O+K_2CO_3$ . The dashed horizontal line refers to the energy minimum of the  $K_4CO_4$  system ( $E_{\min}$ ).

Table 3. Data for structure candidates for  $K_4CO_4$  after local optimizations on ab initio level (HF).

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates	$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]			
		atom	$x$	$y$	$z$		
$P\bar{4}3m$ (215) cubic $Li_4CO_4$ -I	$a = 5.25897$ $\alpha = \beta = \gamma = 90$	C1(1b) O1(4e) K1(4e)	0.5 0.34189 0.79115	0.5 0.34189 0.79115	0.5 0.34189 0.79115	145.446 82.330	-2734.0661
$R\bar{3}m$ (160) trigonal $Li_4CO_4$ -II	$a = 5.16252$ $\alpha = \beta = \gamma = 84.77769$	C1(1a) O1(3b) O2(1a) K1(1a) K2(3b)	0.99961 0.81909 0.16322 0.71409 0.49861	0.99961 0.19316 0.16322 0.71409 0.10286	0.99961 0.81909 0.16322 0.71409 0.49861	135.974 87.864	-2733.8575
$I\bar{4}2m$ (121) tetragonal $Li_4CO_4$ -III	$a = 9.33983$ $c = 5.91476$ $\alpha = \beta = \gamma = 90$	C1(2b) O1(8i) K1(8i)	0 0.08625 0.84168	0 0.08625 0.84168	0.5 0.36522 0.78828	515.960 41.989	-2734.0592
$I\bar{4}2m$ (121) tetragonal $Li_4CO_4$ -IV	$a = 5.08784$ $c = 10.81314$ $\alpha = \beta = \gamma = 90$	C1(2a) O1(8i) K1(8i)	0 0.83761 0.69365	0 0.83761 0.69365	0 0.92081 0.14558	279.911 87.477	-2734.0903
$Cm$ (8) monoclinic $Li_4CO_4$ -V	$a = 8.19217$ $b = 8.29722$ $c = 4.72962$ $\alpha = \gamma = 90$ $\beta = 100.14260$	C1(2a) O1(4b) O2(2a) O3(2a) K1(4b) K2(4b)	0.01715 0.00205 0.89287 0.18803 0.31908 0.14997	0 0.85622 0 0 0.18819 0.69147	0.55182 0.70815 0.30763 0.48175 0.96024 0.39179	316.459 74.468	-2734.0028
$C2$ (5) monoclinic $Li_4CO_4$ -VI	$a = 10.64862$ $b = 5.52021$ $c = 5.63957$ $\alpha = \gamma = 90$ $\beta = 115.92290$	C1(2a) O1(4c) O2(4c) K1(4c) K2(4c)	0 0.91548 0.09037 0.34921 0.13831	0.26132 0.11545 0.41200 0.52577 0.62488	0 0.08008 0.21623 0.51073 0.84647	298.154 80.546	-2734.1076
$R\bar{3}$ (146) trigonal $K_4CO_4$ -I	$a = 5.17681$ $\alpha = \beta = \gamma = 89.95140$	C1(1a) O1(3b) O2(1a) K1(3b) K2(1a)	0.84605 0.68471 0.68219 0.49235 0.13664	0.84605 0.97819 0.68219 0.13352 0.13664	0.84605 0.04222 0.68219 0.61950 0.13664	138.735 85.977	-2734.0430

Table 3. (Continued)

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]		
		atom	x	y	z				
$Cm$ (8) monoclinic $K_4CO_4$ -II	$a = 6.83444$ $b = 7.33625$ $c = 5.54579$ $\alpha = \gamma = 90$ $\beta = 97.87380$	C1(2a)	0.26079	0	0.39829	275.440	-2734.0347		
		O1(2a)	0.13778	0	0.59975				
		O2(4b)	0.21312	0.16517	0.24823	87.318			
		O3(2a)	0.47392	0	0.50055				
		K1(4b)	0.82275	0.79978	0.67143	259.584	-2734.0465		
		K2(2a)	0.45915	0	0.01812				
		K3(2a)	0.88905	0	0.20094				
$I\bar{4}$ (82) tetragonal $K_4CO_4$ -III	$a = 6.81932$ $c = 5.58207$ $\alpha = \beta = \gamma = 90$	C1(2b)	0	0	0.5	94.405			
		O1(8g)	0.03635	0.17543	0.34571				
		K1(8g)	0.90998	0.72416	0.90642	264.731	-2734.0081		
		C1(2a)	0.02472	0	0.49013				
		O1(4b)	0.47402	0.65297	0.63824	90.538			
		O2(2a)	0.25353	0	0.46844				
		O3(2a)	0.89456	0	0.22392				
$Cm$ (8) monoclinic $K_4CO_4$ -IV	$a = 6.45640$ $b = 7.98047$ $c = 5.19308$ $\alpha = \gamma = 90$ $\beta = 98.36010$	K1(4b)	0.59838	0.78465	0.23496	121.415	-2733.6952		
		K2(2a)	0.24363	0	0.96349				
		K3(2a)	0.64390	0	0.71853				
		$R\bar{3}$ (146) trigonal $K_4CO_4$ -VI	$a = 4.95471$ $\alpha = \beta = \gamma = 87.99350$	C1(1a)	0.51548	0.51548	0.51548	81.922	
				O1(3b)	0.59943	0.32848	0.82533		
				O2(1a)	0.31269	0.31269	0.31269	243.722	-2733.9820
				K1(3b)	0.10425	0.31483	0.80713		
K2(1a)	0.81517			0.81517	0.81517	96.125			
C1(2b)	1/4			1/4	3/4				
$P4_2/n$ (86) tetragonal $K_4CO_4$ -VII	$a = 6.66640$ $c = 5.48419$ $\alpha = \beta = \gamma = 90$			O1(8g)	0.17621	0.06975	0.58391	0.86563	
		K1(8g)	0.68160	0.45697	0.86563				

between 23 GPa (DFT-B3LYP) and 33 GPa (HF). Upon increasing the pressure we find that the  $K_4CO_4$ -III modification should exhibit a phase transition to the  $K_4CO_4$ -VII structure type at 40–45 GPa (cf. Figure 8). Note that in the same range of pressures the carbonate  $\gamma$ - $Na_2CO_3$  modifica-

tion undergoes a phase transition to the  $K_2CO_3$ -Type-11 modification. The possible high-pressure structures in the  $K_4CO_4$  system are shown below (see Figures 16 and 17). The structures belong to the  $I\bar{7}2(II)$  ( $K_4CO_4$ -III) and  $oC2$  ( $K_4CO_4$ -VII) arrangement of heterocubanes (see refs. [25] and [26]). Table 3 and Table S1.3 in the Supporting Information show structural data, minimum volumes, bulk moduli and energies of the selected structure candidates for  $K_4CO_4$  system after local optimizations on Hartree-Fock and DFT-B3LYP level, respectively.

*Results restricted to  $Rb_4CO_4$ :* When performing ab initio calculations for  $Rb_4CO_4$ , which contains heavy Rb atoms, we encounter potential problems associated with the choice of the basis sets, and, possibly, with relativistic effects. As in the case of  $Rb_2O$  and  $Rb_2CO_3$ , we have employed the ECP28MBW “Stuttgart/Cologne based”<sup>[30]</sup> pseudo-potential basis set (PPBS). For the

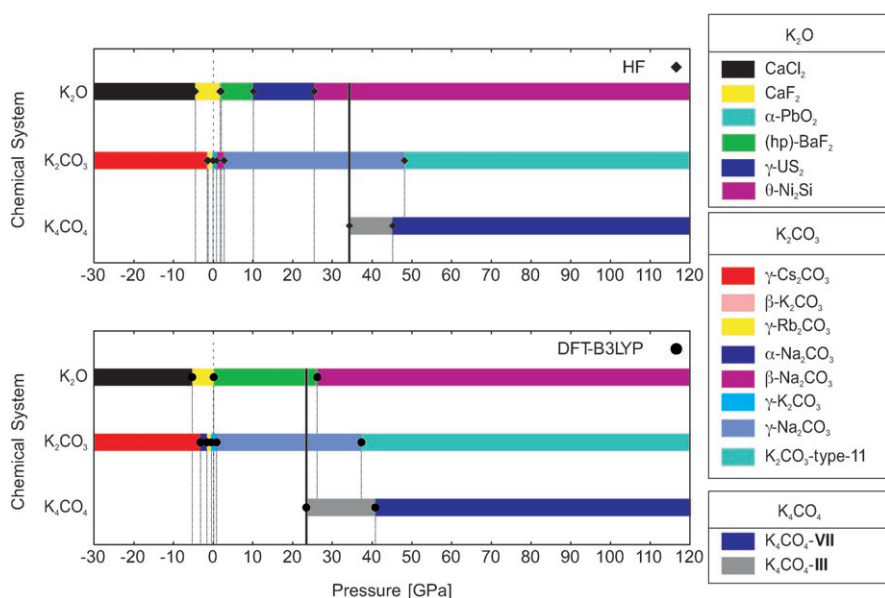


Figure 8. Low-temperature modifications of  $K_4CO_4$  as function of pressure in equilibrium with the solid state reaction  $K_2O + K_2CO_3$ . Only the modifications with the lowest enthalpy are depicted. Upper box: HF. Lower box: DFT-B3LYP.

Table 4. Data for structure candidates for  $\text{Rb}_4\text{CO}_4$  after local optimizations on ab initio level (HF).

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	$x$	$y$	$z$		
$P\bar{4}3m$ (215) cubic $\text{Li}_4\text{CO}_4$ - <b>I</b>	$a = 5.55848$	C1(1b)	0.5	0.5	0.5	171.739	−432.7075
	$\alpha = \beta = \gamma = 90$	O1(4e)	0.34806	0.34806	0.34806	71.744	
		Rb1(4e)	0.78992	0.78992	0.78992		
$R\bar{3}m$ (160) trigonal $\text{Li}_4\text{CO}_4$ - <b>II</b>	$a = 6.27378$	C1(1a)	0.99961	0.99961	0.99961	210.809	−432.0655
	$\alpha = \beta = \gamma = 69.98695$	O1(3b)	0.81909	0.19316	0.81909	49.616	
		O2(1a)	0.16322	0.16322	0.16322		
		Rb1(1a)	0.71409	0.71409	0.71409		
		Rb2(3b)	0.49861	0.10286	0.49861		
$I\bar{4}2m$ (121) tetragonal $\text{Li}_4\text{CO}_4$ - <b>III</b>	$a = 8.97453$	C1(2b)	0	0	0.5	436.720	−432.7467
	$c = 5.42225$	O1(8i)	0.09334	0.09334	0.35101	55.953	
	$\alpha = \beta = \gamma = 90$	Rb1(8i)	0.82352	0.82352	0.85641		
$I\bar{4}2m$ (121) tetragonal $\text{Li}_4\text{CO}_4$ - <b>IV</b>	$a = 5.35530$	C1(2a)	0	0	0	358.189	−432.7204
	$c = 12.48952$	O1(8i)	0.84501	0.84501	0.93246	68.888	
	$\alpha = \beta = \gamma = 90$	Rb1(8i)	0.70283	0.70283	0.13724		
	$a = 8.65529$	C1(2a)	0.00657	0	0.49656	373.219	
	$b = 8.76626$	O1(4b)	0.99940	0.82590	0.71390	56.408	
$Cm$ (8) monoclinic $\text{Li}_4\text{CO}_4$ - <b>V</b>	$c = 4.99700$	O2(2a)	0.83315	0	0.21440		−432.2878
	$\alpha = \gamma = 90$	O3(2a)	0.19434	0	0.35368		
	$\beta = 100.14260$	Rb1(4b)	0.80546	0.69459	0.00932		
		Rb2(4b)	0.69823	0.19818	0.47525		
		C1(2a)	0	0.92976	0	379.398	
$C2$ (5) monoclinic $\text{Li}_4\text{CO}_4$ - <b>VI</b>	$a = 11.51402$	O1(4c)	0.92004	0.06662	0.80202	61.829	−432.7495
	$b = 5.98847$	O2(4c)	0.07969	0.79521	0.93402		
	$c = 6.11798$	Rb1(4c)	0.14869	0.69849	0.46219		
	$\alpha = \gamma = 90$	Rb2(4c)	0.86013	0.29905	0.11760		
	$\beta = 115.92290$	C1(2b)	0	0	0.5	336.131	
$I\bar{4}2m$ (121) tetragonal $\text{Rb}_4\text{CO}_4$ - <b>I</b>	$a = 5.71070$	O1(8i)	0.35097	0.35097	0.91664	73.537	−432.7332
	$c = 10.30694$	Rb1(8i)	0.79794	0.79794	0.14703		
	$\alpha = \beta = \gamma = 90$	C1(2a)	0.46097	0	0.27718	377.390	
	$a = 6.74926$	O1(4b)	0.90571	0.62834	0.40099	62.756	
	$b = 9.18786$	O2(2a)	0.67300	0	0.24806		
	$c = 6.08714$	O3(2a)	0.35638	0	0.06563		
	$\alpha = \gamma = 90$	Rb1(4b)	0.09280	0.22635	0.07654		
	$\beta = 91.18920$	Rb2(2a)	0.61257	0	0.71980		
		Rb3(2a)	0.05874	0	0.49529		
		C1(1a)	0.20172	0.20172	0.20172	162.588	
$R\bar{3}$ (146) trigonal $\text{Rb}_4\text{CO}_4$ - <b>III</b>	$a = 5.45813$	O1(3b)	0.32205	0.05017	0.39466	78.548	−432.6790
	$\alpha = \beta = \gamma = 90.46120$	O2(1a)	0.04315	0.04315	0.04315		
		Rb1(3b)	0.98349	0.50192	0.84502		
		Rb2(1a)	0.49822	0.49822	0.49822		
		C1(2a)	0.96147	0	0.42202	372.618	
$Cm$ (8) monoclinic $\text{Rb}_4\text{CO}_4$ - <b>IV</b>	$a = 6.79048$	O1(2a)	0.85319	0	0.19346	63.767	−432.7133
	$b = 9.51845$	O2(2a)	0.17173	0	0.39255		
	$c = 5.78647$	O3(4b)	0.91091	0.87438	0.54675		
	$\alpha = \gamma = 90$	Rb1(4b)	0.09914	0.72794	0.22124		
	$\beta = 94.94170$	Rb2(2a)	0.13661	0	0.86776		
		Rb3(2a)	0.56346	0	0.64152		
$I222$ (23) orthorhombic $\text{Rb}_4\text{CO}_4$ - <b>VI</b>	$a = 5.40585$	C1(2c)	0	0	0.5	339.586	−432.7397
	$b = 10.50963$	O1(8k)	0.34430	0.58091	0.14104	72.460	
	$c = 5.97721$	Rb1(8k)	0.82258	0.35170	0.72180		
$P\bar{4}$ (81) tetragonal $\text{Rb}_4\text{CO}_4$ - <b>VII</b>	$a = 6.57331$	C1(1b)	0	0	0.5	137.816	−432.0784
	$c = 3.18956$	O1(4 h)	0.78245	0.96102	0.82091	85.803	
	$\alpha = \beta = \gamma = 90$	Rb1(4 h)	0.45965	0.77965	0.26688		
$Amm2$ (38) orthorhombic $\text{Rb}_4\text{CO}_4$ - <b>VIII</b>	$a = 7.03882$	C1(2b)	0.5	0	0.59618	283.326	−432.1556
	$b = 6.05810$	O1(4e)	0.5	0.25874	0.25090	77.964	
	$c = 6.64432$	O2(4c)	0.29329	0	0.44249		
	$\alpha = \beta = \gamma = 90$	Rb1(4d)	0	0.74594	0.23866		
		Rb2(4c)	0.71185	0	0.99873		
$P2_1$ (4) monoclinic $\text{Rb}_4\text{CO}_4$ - <b>IX</b>	$a = 8.80430$	C1(2a)	0.73622	0.27119	0.29928	317.204	−432.7167
	$b = 5.26961$	O1(2a)	0.64509	0.49302	0.23290	78.758	
	$c = 6.83880$	O2(2a)	0.65657	0.03345	0.24321		
	$\alpha = \gamma = 90$	O3(2a)	0.75563	0.28285	0.51502		



Table 4. (Continued)

Space group (no.) crystal system, type	Lattice constants ( $a, b, c$ [Å]; $\alpha, \beta, \gamma$ [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				$V_{\min}$ [Å <sup>3</sup> ]	$E_{\min}$ [a.u.]
		atom	x	y	z		
<i>Cm</i> (8) monoclinic <b>Rb<sub>4</sub>CO<sub>4</sub>-XI</b>	$\beta = 91.31550$	O4(2a)	0.88695	0.27748	0.20731	321.600 76.906	-432.6779
		Rb1(2a)	0.38615	0.76205	0.12444		
		Rb2(2a)	0.42062	0.25194	0.42743		
		Rb3(2a)	0.08862	0.29586	0.58283		
		Rb4(2a)	0.16520	0.26545	0.04059		
	$a = 6.92575$ $b = 8.52253$ $c = 5.65858$ $\alpha = \gamma = 90$ $\beta = 103.8027$	C1(2a)	0.65347	0	0.27702		
		O1(4b)	0.60124	0.85744	0.40320		
		O2(2a)	0.87194	0	0.29190		
		O3(2a)	0.54217	0	0.01427		
		Rb1(2a)	0.86224	0	0.76792		
<i>C2</i> (5) monoclinic <b>Rb<sub>4</sub>CO<sub>4</sub>-XII</b>	$a = 12.47167$ $b = 3.18265$ $c = 9.04295$ $\alpha = \gamma = 90$ $\beta = 128.45410$	Rb2(2a)	0.27398	0	0.53325		
		Rb3(4b)	0.25042	0.21097	0.05684		
		C1(2a)	0	0.14944	0		
		O1(4c)	0.87189	0.82302	0.80989		
		O2(4c)	0.07454	0.47373	0.92464		
		Rb1(4c)	0.33286	0.38468	0.22435		
Rb2(4c)	0.11936	0.34881	0.44428				

most promising structure types of the Rb<sub>4</sub>CO<sub>4</sub> system,  $E(V)$  curves and structure data are shown in the Figure 9 and Table 4 (for DFT-B3LYP data see Supporting Information Figure S1.7 and the Table S1.4). Similar to the case of potassium, in the rubidium-based mixture of oxides and carbonates, many phase transitions occur in the pressure range from -5 GPa to +5 GPa. Once again this should not affect our ability to predict high-pressure transitions to the ther-

modynamically stable orthocarbonate phase. As one can see in Figure 10, in the Rb<sub>4</sub>CO<sub>4</sub> system the first transition from Rb<sub>2</sub>O (in the  $\gamma$ -US<sub>2</sub> phase) plus Rb<sub>2</sub>CO<sub>3</sub> (in the  $\gamma$ -K<sub>2</sub>CO<sub>3</sub> phase) to the Rb<sub>4</sub>CO<sub>4</sub>-IX modification should occur between 22 GPa (DFT-B3LYP) and 32 GPa (HF). The Rb<sub>4</sub>CO<sub>4</sub>-IX modification upon increasing pressure transforms into the Rb<sub>4</sub>CO<sub>4</sub>-XI modification between 44 GPa (DFT-B3LYP) and 52 GPa (HF). This time the predicted

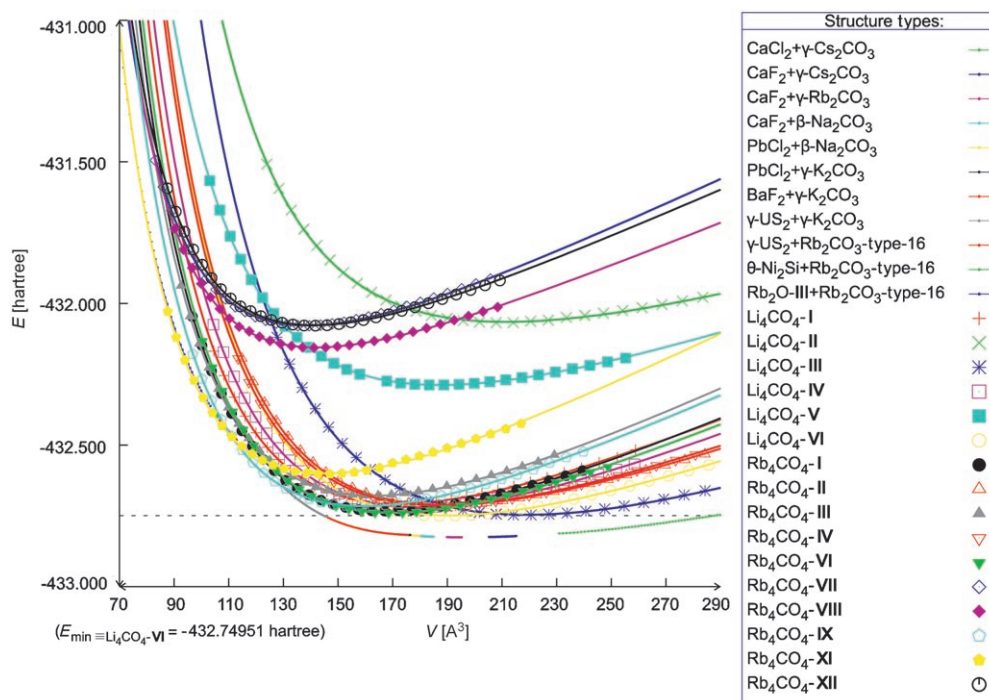


Figure 9.  $E(V)$  curves for selected structure candidates calculated on an ab initio level (HF) in the Rb<sub>4</sub>CO<sub>4</sub> system together with the combined curve for Rb<sub>2</sub>O + Rb<sub>2</sub>CO<sub>3</sub>. The dashed horizontal line refers to the energy minimum of the Rb<sub>4</sub>CO<sub>4</sub> system ( $E_{\min}$ ).

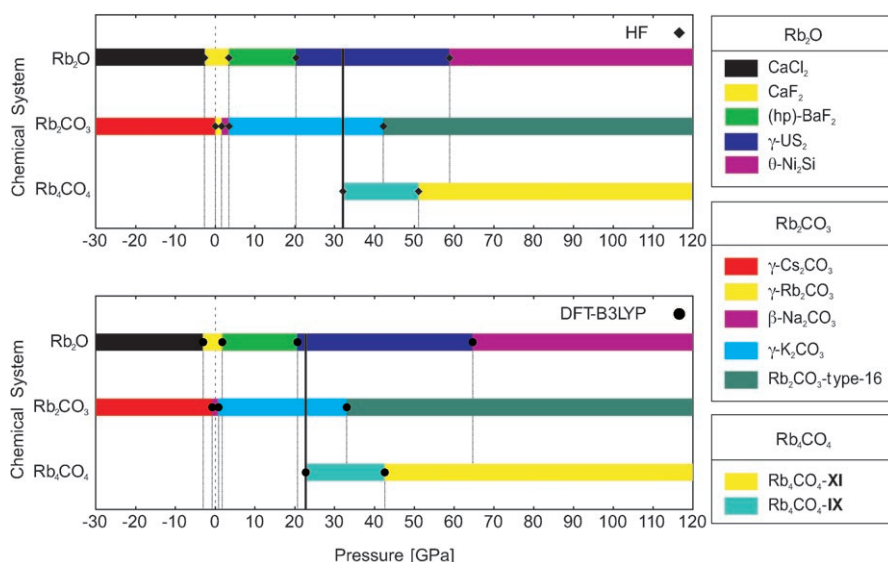


Figure 10. Low-temperature modifications of  $\text{Rb}_4\text{CO}_4$  as function of pressure in equilibrium with the solid state reaction  $\text{Rb}_2\text{O} + \text{Rb}_2\text{CO}_3$ . Only the modifications with the lowest enthalpy are depicted. Upper box: HF. Lower box: DFT-B3LYP.

structure does not fit into the nomenclature of spatial arrangements of heterocubanes. Table 4 and Table S1.4 in the Supporting Information show structural data, minimum volumes, bulk moduli and energies of the selected structure candidates for  $\text{Rb}_4\text{CO}_4$  system after local optimizations on Hartree–Fock and DFT-B3LYP level.

**Results restricted to  $\text{Cs}_4\text{CO}_4$ :** For the same reason as in the case of rubidium, we expect relativistic effects to be possibly

of relevance for cesium-based compounds. Thus, we perform all calculations employing an optimized ECP46MWB “Stuttgart/Cologne based” basis set. For the most promising structure types of the  $\text{Cs}_4\text{CO}_4$  system,  $E(V)$  curves and corresponding structure data are shown in Figure 11 and Table 5 (for DFT-B3LYP data see Supporting Information Figure S1.9 and Table S1.5). Considering the transition pressures in Figure 12 we find, for both computational procedures (HF and DFT-B3LYP), that in this system the transition to the possible orthocarbonate modification probably will require pressures in excess of 200 GPa. Of course, according to our experience, we cannot fully trust in our calculations in the range of such extremely high pressures, especially if the range must be extrapolated using a fitting formula. We should note that in order to get convergence of the ab initio calculations for several extremely compressed structures under extreme pressures one should perform a re-optimization of the normally frozen basis set for small cell volume, in addition to the regular relaxation of the structure. However, this involves very time-consuming computations, and we can estimate, according to our experi-

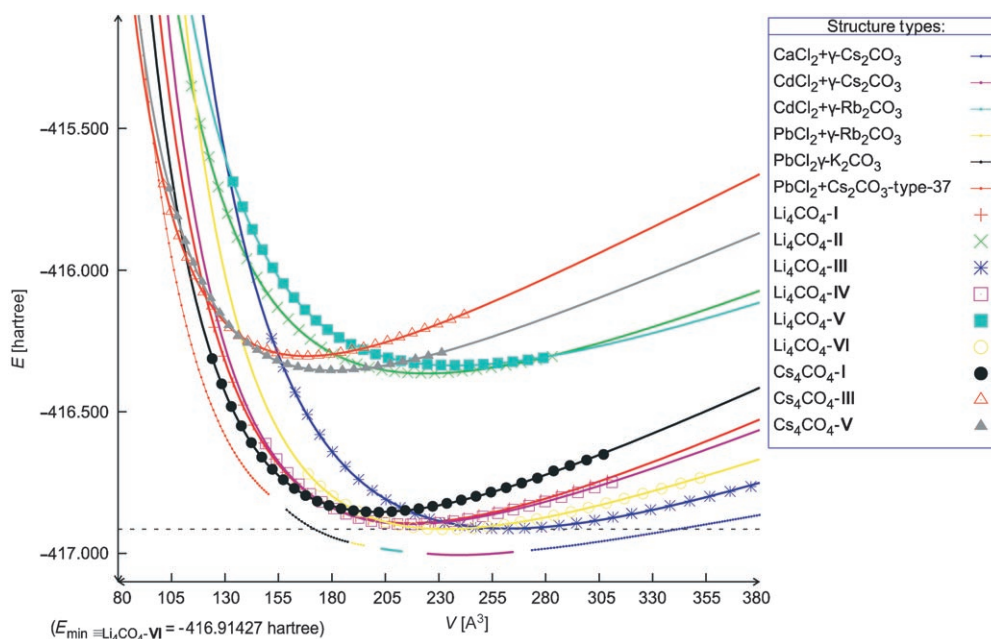


Figure 11.  $E(V)$  curves for selected structure candidates calculated on ab initio level (HF) in the  $\text{Cs}_4\text{CO}_4$  system together with the combined curve for  $\text{Cs}_2\text{O} + \text{Cs}_2\text{CO}_3$ . The dashed horizontal line refers to the energy minimum of the  $\text{Cs}_4\text{CO}_4$  system ( $E_{\min}$ ).

Table 5. Data for structure candidates for Cs<sub>4</sub>CO<sub>4</sub> after local optimizations on ab initio level (HF).

Space group (no.) crystal system, type	Lattice constants ( <i>a, b, c</i> [Å]; <i>α, β, γ</i> [°])	Atom (multiplicity, Wyckoff letter), relative coordinates				<i>V</i> <sub>min</sub> [Å <sup>3</sup> ]	<i>E</i> <sub>min</sub> [a.u.]
		atom	<i>x</i>	<i>y</i>	<i>z</i>		
<i>P</i> 4̄3 <i>m</i> (215) cubic Li <sub>4</sub> CO <sub>4</sub> - <b>I</b>	<i>a</i> = 5.99260	C1(1b)	0.5	0.5	0.5	215.201	-416.8931
	<i>α</i> = <i>β</i> = <i>γ</i> = 90	O1(4e)	0.35881	0.35881	0.35881	59.526	
		Cs1(4e)	0.78309	0.78309	0.78309		
<i>R</i> 3 <i>m</i> (160) trigonal Li <sub>4</sub> CO <sub>4</sub> - <b>II</b>	<i>a</i> = 6.09349	C1(1a)	0.99961	0.99961	0.99961	223.599	-416.3640
	<i>α</i> = <i>β</i> = <i>γ</i> = 84.77769	O1(3b)	0.81909	0.19316	0.81909	50.967	
		O2(1a)	0.16322	0.16322	0.16322		
		Cs1(1a)	0.71409	0.71409	0.71409		
		Cs2(3b)	0.49861	0.10286	0.49861		
<i>I</i> 4̄2 <i>m</i> (121) tetragonal Li <sub>4</sub> CO <sub>4</sub> - <b>III</b>	<i>a</i> = 9.53209	C1(2b)	0	0	0.5	523.278	-416.9124
	<i>c</i> = 5.75912	O1(8i)	0.08862	0.08862	0.35686	47.457	
	<i>α</i> = <i>β</i> = <i>γ</i> = 90	Cs1(8i)	0.82704	0.82704	0.84449		
<i>I</i> -42 <i>m</i> (121) tetragonal Li <sub>4</sub> CO <sub>4</sub> - <b>IV</b>	<i>a</i> = 5.70547	C1(2a)	0	0	0	433.149	-416.8969
	<i>c</i> = 13.30622	O1(8i)	0.85318	0.85318	0.93648	57.773	
	<i>α</i> = <i>β</i> = <i>γ</i> = 90	Cs1(8i)	0.71283	0.71283	0.13753		
	<i>a</i> = 9.37929	C1(2a)	0.00657	0	0.49656	474.931	
	<i>b</i> = 9.49956	O1(4b)	0.99940	0.82590	0.71390	45.819	
<i>Cm</i> (8) monoclinic Li <sub>4</sub> CO <sub>4</sub> - <b>V</b>	<i>c</i> = 5.41499	O2(2a)	0.83315	0	0.21440		-416.3364
	<i>α</i> = <i>γ</i> = 90	O3(2a)	0.19434	0	0.35368		
	<i>β</i> = 100.14260	Cs1(4b)	0.80546	0.69459	0.00932		
		Cs2(4b)	0.69823	0.19817	0.47525		
		C1(2a)	0	0.91735	0	465.675	
		O1(4c)	0.93850	0.05027	0.82851	51.964	
		O2(4c)	0.07685	0.78708	0.92336		
		Cs1(4c)	0.13463	0.71710	0.42652		
		Cs2(4c)	0.85621	0.31113	0.10092		
		C1(1a)	0.82954	0.82954	0.82954	201.430	
<i>R</i> 3 (146) trigonal Cs <sub>4</sub> CO <sub>4</sub> - <b>I</b>	<i>a</i> = 5.86328	O1(1a)	0.97451	0.97451	0.97451	64.026	-416.8541
	<i>α</i> = <i>β</i> = <i>γ</i> = 88.76340	O2(3b)	0.97729	0.71699	0.65330		
		Cs1(3b)	0.53521	0.04319	0.19094		
		Cs2(1a)	0.53964	0.53964	0.53964		
		C1(2b)	0	0.99888	0.5	335.199	
<i>C2</i> (5) monoclinic Cs <sub>4</sub> CO <sub>4</sub> - <b>III</b>	<i>a</i> = 12.75255	O1(4c)	0.57168	0.19662	0.42260	73.627	-416.3038
	<i>b</i> = 3.44604	O2(4c)	0.38126	0.79262	0.32367		
	<i>c</i> = 9.27353	Cs1(4c)	0.38517	0.26635	0.06348		
	<i>α</i> = <i>γ</i> = 90	Cs2(4c)	0.17759	0.24831	0.29000		
	<i>β</i> = 124.66330	C1(4c)	0.20620	0.47656	0.14068	721.164	
<i>C2</i> (5) monoclinic Cs <sub>4</sub> CO <sub>4</sub> - <b>V</b>	<i>a</i> = 13.27106	O1(4c)	0.33002	0.44273	0.98511	59.818	-416.3543
	<i>b</i> = 13.27412	O2(4c)	0.21071	0.47956	0.58343		
	<i>c</i> = 4.09379	O3(4c)	0.61619	0.88139	0.00995		
	<i>α</i> = <i>γ</i> = 90	O4(4c)	0.16997	0.59996	0.98213		
	<i>β</i> = 90.20580	Cs1(4c)	0.70976	0.27645	0.50761		
		Cs2(2b)	0	0.97318	0.5		
		Cs3(2b)	0	0.29765	0.5		
		Cs4(2a)	0	0.76315	0		
		Cs5(4c)	0.62820	0.64677	0.98582		
		Cs6(2b)	0	0.55229	0.5		

ence, that the reliability of our prediction of transition pressures in this system to be sufficiently high at least up to 150 GPa. We further note that our calculated transition pressures in the range of 220 to 310 GPa are probably the upper limit of the transition pressure in Cs<sub>4</sub>CO<sub>4</sub> system. We can roughly estimate that the actual pressure in the case of Cs<sub>4</sub>CO<sub>4</sub> could be up to 50 GPa lower than those predicted by our calculations using frozen basis sets. As in the case of Rb<sub>4</sub>CO<sub>4</sub> the predicted structure of the Cs<sub>4</sub>CO<sub>4</sub> does not fit into the nomenclature of spatial arrangements of heterocubanes. Table 5 and Table S1.5 in the Supporting Information show structural data, minimum volumes, bulk moduli and

energies of the selected structure candidates for Cs<sub>4</sub>CO<sub>4</sub> system after local optimizations on Hartree–Fock and DFT–B3LYP level.

## Discussion

In this work we have presented structure candidates for the alkali metal orthocarbonates at low temperatures and pressures up to 250 GPa. We have computed transition pressures for the solid state reaction A<sub>2</sub>O + A<sub>2</sub>CO<sub>3</sub> ⇌ A<sub>4</sub>CO<sub>4</sub> (A = Li, Na, K, Rb, and Cs). The results of the calculations show

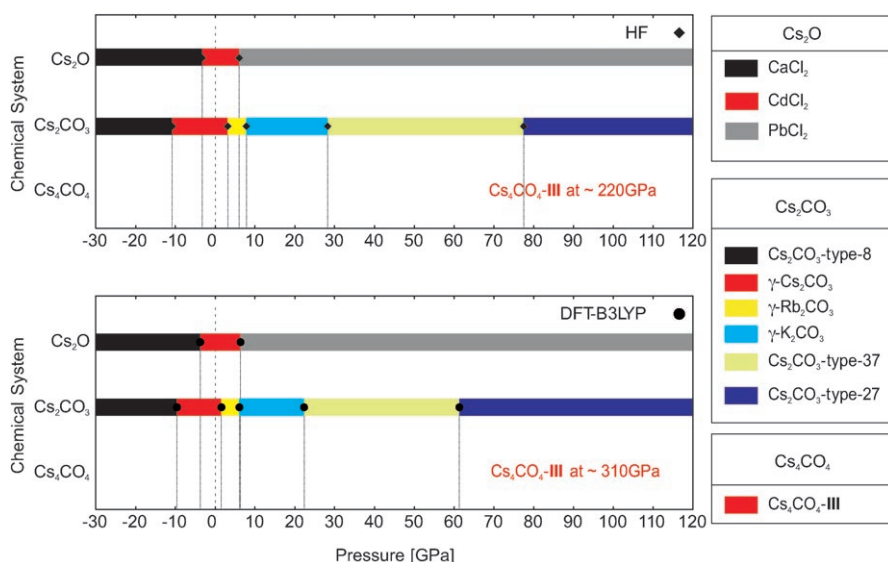


Figure 12. Low-temperature modifications of  $\text{Cs}_4\text{CO}_4$  as function of pressure in equilibrium with the solid state reaction  $\text{Cs}_2\text{O} + \text{Cs}_2\text{CO}_3$ . Only the modifications with the lowest enthalpy are depicted. Upper box: HF. Lower box: DFT-B3LYP.

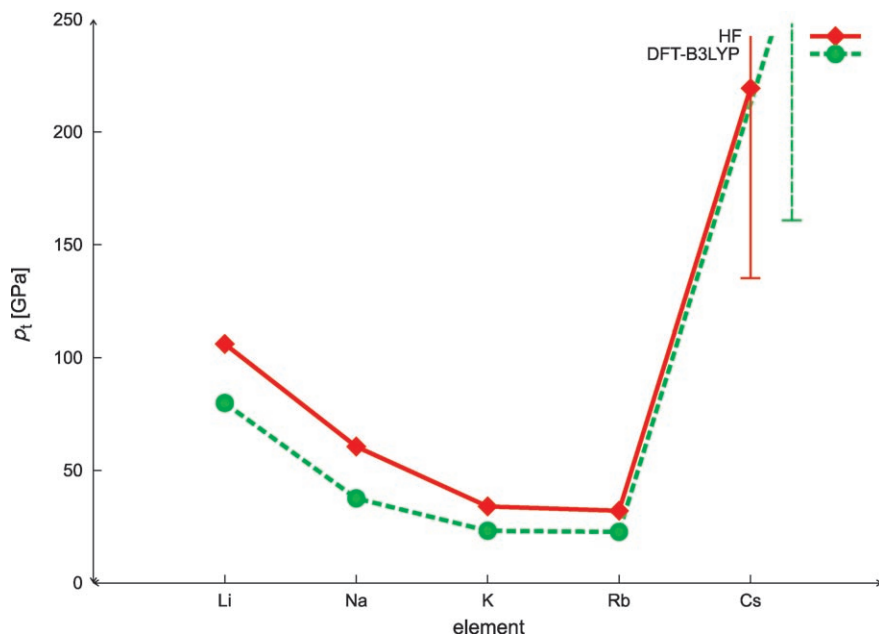


Figure 13. Transition pressures between the mixture  $\text{A}_2\text{O} + \text{A}_2\text{CO}_3$  and the orthocarbonate  $\text{A}_4\text{CO}_4$ .

that, at zero temperature and zero pressure, there exists only the mixture of the corresponding most stable modifications in the system  $\text{A}_2\text{O}$  and  $\text{A}_2\text{CO}_3$ . We find that potassium and rubidium show relatively low transition pressures from  $\text{A}_2\text{O}$ -plus- $\text{A}_2\text{CO}_3$  to the hypothetical modifications of  $\text{A}_4\text{CO}_4$ . Considering the cation size, one would expect the lithium orthocarbonate to have the lowest pressure of formation, while when arguing from alkali oxide basicity, cesium orthocarbonate should appear first as function of pressure. Actually the opposite trend has been found: plotting the cations versus transition pressure to the hypotheti-

cal modifications in the  $\text{A}_4\text{CO}_4$  system we find a minimum for K and Rb (see Figure 13).

In order to gain some estimate for the uncertainty in the theoretical results we have employed two different Hamiltonians (HF and DFT) while using the same combinations of slightly re-optimized basis sets for all three classes of systems: oxides, carbonates and orthocarbonates. As we have discussed in reference [10,11] and [29], essentially all volumes calculated with HF are somewhat larger than the experimental ones, and cells computed with DFT-B3LYP are close to or smaller than experimental values, respectively. This fits our general observation in all of the system we have studied. This also suggests that the experimental transition pressure should lie between the ones calculated with HF (upper limit) and DFT (lower limit).

As we commented in an earlier paper,<sup>[27]</sup> within a given group of ab initio methods (HF and DFT) there exists sometimes a noticeable dependence on the choice of basis sets. For this reason we have performed some additional optimizations of the outermost coefficients of the basis sets<sup>2</sup> in a few cases. In order to avoid the problem of basis set comparability while studying rather different systems with the same overall composition  $\text{A}_4\text{CO}_4$  and  $\text{A}_2\text{O}$  plus  $\text{A}_2\text{CO}_3$ , basis sets employed in calculations of the orthocarbonates are almost the same as the ones for the oxides and carbonates.

We should note that we cannot guarantee that our global search procedure will identify all possible candidates for high-pressure structures. Considering the complexity of the

<sup>2</sup> The main basis set optimization task had been performed during earlier studies in other systems. For example, optimizations and testing of the alkali metal basis sets was mostly accomplished in the system of alkali metal sulfides (see ref. [27]). Then, fine tuning of the alkali metal basis sets and optimization of the oxygen basis set has been performed in the alkali metal oxides (see ref. [11]). Finally, the main optimization of the carbon basis set has been done in the alkali metal carbonates (see ref. [10]).



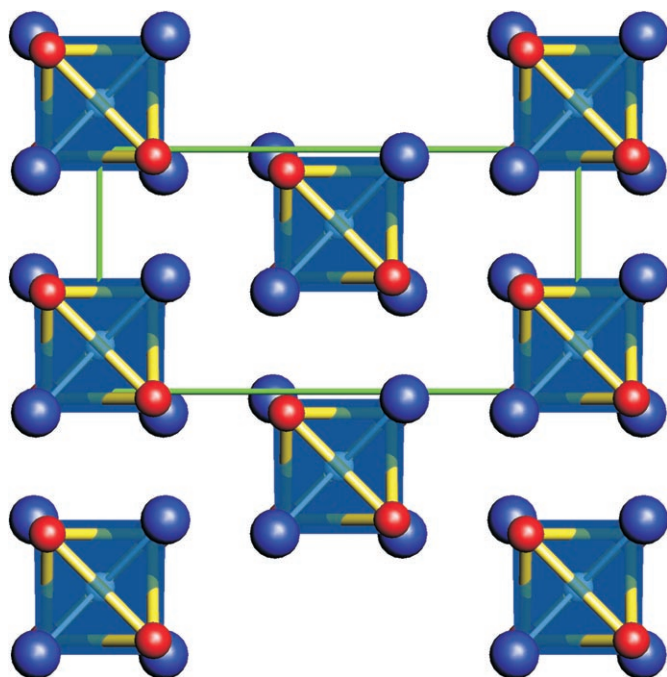


Figure 14. High-pressure modification of  $\text{Li}_4\text{CO}_4$  system:  $\text{Li}_4\text{CO}_4\text{-X}$ . Little (red) spheres refer to oxygen, big (blue) spheres refer to the alkali metal ( $A=\text{Li, Na, K, Rb, Cs}$ ), and little (white) spheres in the center of the oxygen tetrahedra refer to carbon.

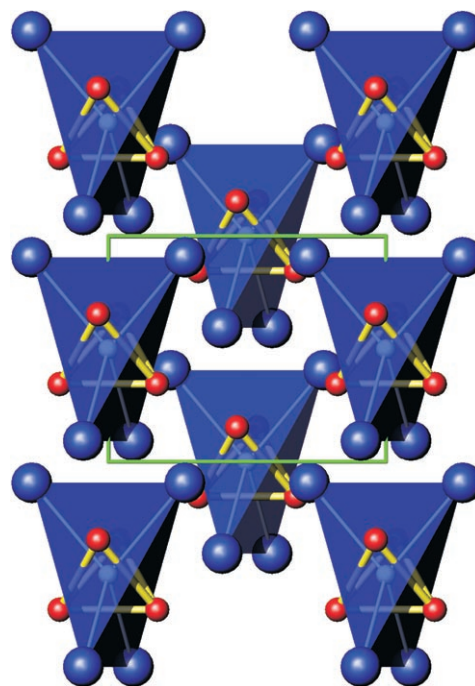


Figure 16. High-pressure modification of  $\text{K}_4\text{CO}_4$  system:  $\text{K}_4\text{CO}_4\text{-III}$ . For notation see Figure 14.

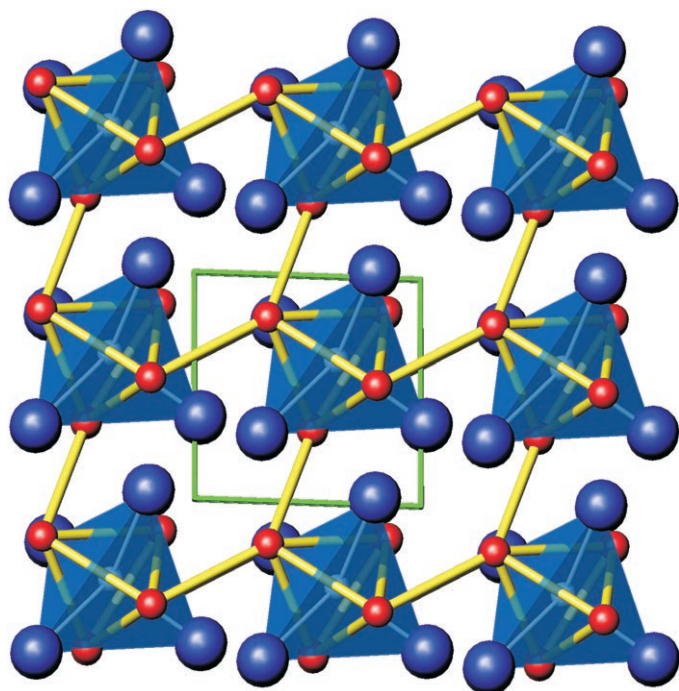


Figure 15. High-pressure modification of  $\text{Na}_4\text{CO}_4$  system:  $\text{Na}_4\text{CO}_4\text{-IV}$ . For notation see Figure 14.

landscapes, missing a relevant candidate is most likely to happen for the orthocarbonates and less likely so for the oxides and carbonates, in particular since already employing

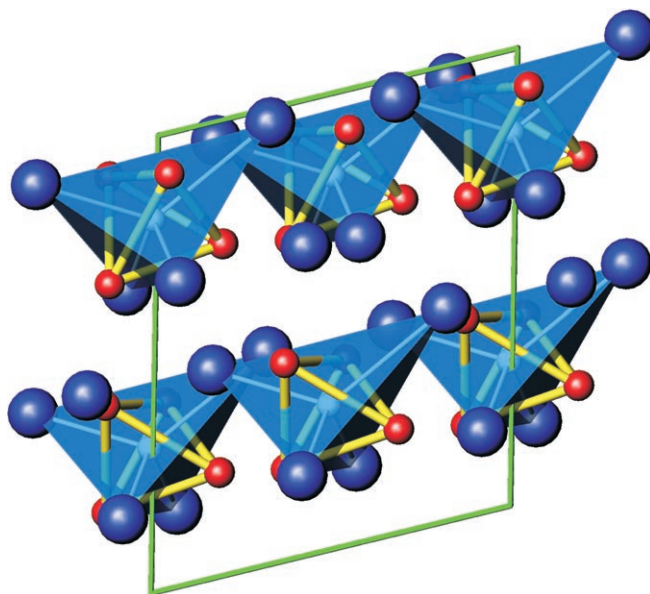


Figure 17. High-pressure modification of  $\text{K}_4\text{CO}_4$  system:  $\text{K}_4\text{CO}_4\text{-VII}$ . For notation see Figure 14.

three formula units during the global optimization of the orthocarbonates proved to be computationally very expensive. However, if another thermodynamically more stable candidate existed among the orthocarbonates, then this would actually result in a lower transition pressure. Thus, we suggest that our predicted pressures are most likely upper limits for

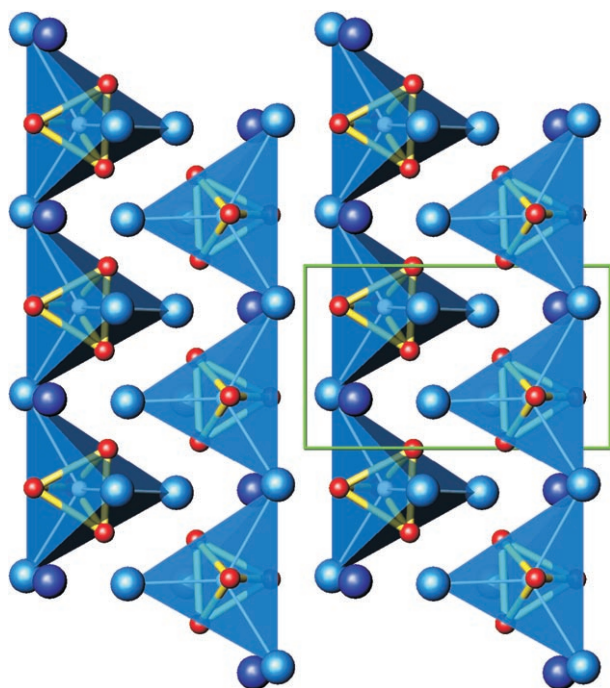


Figure 18. High-pressure modification of  $\text{Rb}_4\text{CO}_4$  system:  $\text{Rb}_4\text{CO}_4\text{-IX}$ . For notation see Figure 14.

the actual transition pressures (even though this would regrettably imply that we would not have found the correct modification!).

Finally, there is the surprisingly high expected transition pressure for  $\text{Cs}_4\text{CO}_4$ . Possible sources of error associated with the *ab initio* calculation of  $\text{Cs}_4\text{CO}_4$  are relativistic effects and dispersive interactions, which are of particular importance for Cs, and which can only be partly accounted for in the choice of basis sets and pseudopotentials. Furthermore, experience has shown that the extrapolation of the fit of the  $E(V)$  curve with the Murnaghan formula can be very sensitive to the number of calculated data points, in particular for very small volumes and high pressures. Finally, a possible reason might be the relatively large size of the cesium atoms, which do not allow sufficiently regular joint packing of the  $\text{CO}_4$  units and the Cs atoms, and thus forces the system into energetically unfavorable arrangements compared to the ones exhibited by for example,  $\text{K}_4\text{CO}_4$  or  $\text{Rb}_4\text{CO}_4$ .

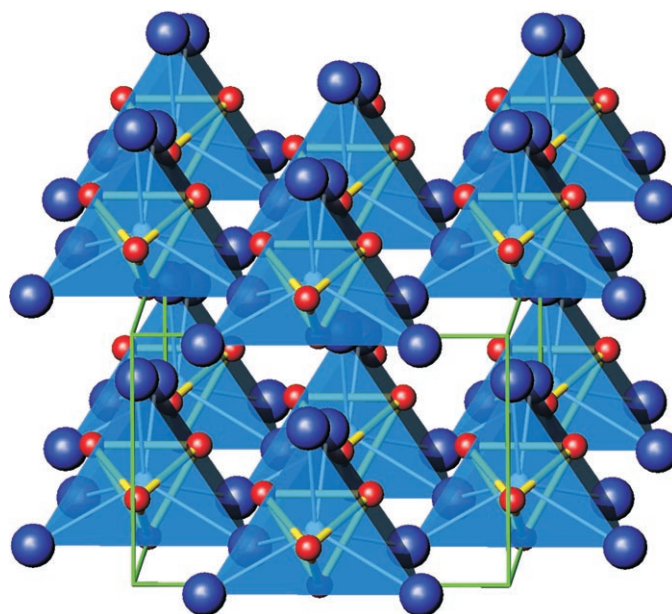


Figure 19. High-pressure modification of  $\text{Rb}_4\text{CO}_4$  system:  $\text{Rb}_4\text{CO}_4\text{-XI}$ . For notation see Figure 14.

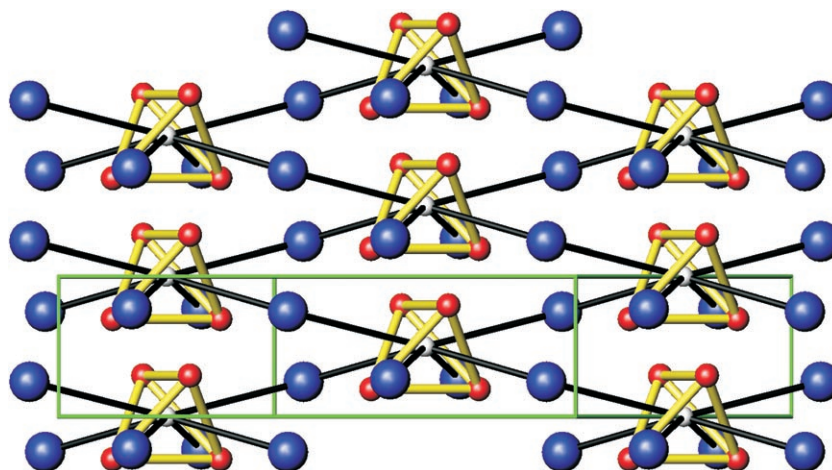


Figure 20. High-pressure modification of  $\text{Cs}_4\text{CO}_4$  system:  $\text{Cs}_4\text{CO}_4\text{-III}$ . For notation see Figure 14.

## Acknowledgement

Funding was provided by the BMBF via grant No. 03C0352. We would like to thank J. Nuss for many valuable discussions.

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Received: November 15, 2006  
Published online: June 21, 2007